

FIR FILTER AND SETTING METHOD OF COEFFICIENT THEREOF

BACKGROUND OF THE INVENTION

5 1. Field of the Invention

The present invention relates to an FIR filter and setting method of coefficients of the FIR filter that are necessary for digital signal processing.

2. Description of the Related Art

10 In the digital signal processing for picture and/or voice, filter processing is often used. Linear-phase FIR (Finite Impulse Response) filter is often utilized as the filter for digital signal processing of picture and/or voice in that the linear-phase FIR filter
15 has the characteristics that its number of taps is finite and has linear-phase.

Fig.1 is a view illustrating circuit configuration of transversal type filter of the linear-phase FIR filter.

20 The linear-phase FIR filter 1, as illustrated in Fig.1, has $(n - 1)$ delay units 2-1 to 2-(n-1) that constitute a shift register connected to an input terminal T_{IN} with cascade connection, n multipliers 3-1 to 3-n for multiplying signal input to the input terminal
25 T_{IN} and output signals of respective delay units 2-1 to

2-(n-1) by filter coefficients $h(0)$ to $h(n-1)$ respectively, and an adder 4 for adding n output signals of the multipliers 3-1 to 3-n to output to an output terminal T_{OUT} .

5 As typical method for designing such the linear-phase FIR filter, for instance, there is known Remez Exchange algorithms which Parks, T.W. and McCleLLan, J.H. et al. apply it to the linear-phase FIR filter (Parks, T.W. and McClellan, J.H.: "Chebyshev Approximation for
10 Non-recursive Digital Filters with Linear Phase", IEEE Trans. Circuit Theory, CT-19, 2, pp.189-194, 1972, as well as Rabiner, L.R., McClellan, J.H. and Parks, T.W.: "FIR Digital Filter Design Techniques Using Weighted Chebyshev Approximation", Proc. IEEE, Vol 63, April, pp.595-610,
15 1975).

The Remez Exchange algorithms is an algorithms in which a weighted approximation error is approximated such that the weighted approximation error is made to configure equi-ripple to the desired amplitude
20 characteristics.

There is known a resolution conversion of picture that utilizes the sampling rate conversion as the application of the filter processing using the linear-phase FIR filter.

25 In this resolution conversion, multi-rate filter

which has an interpolator, a decimeter and the linear-phase FIR filter as element-technique is employed (see, P.P.Vaidyanathan: "Multirate System and Filter Banks", Prentice Hall, 1992).

5 In use of the multi-rate filter, generally, the linear-phase FIR filter is made to use in such a way as to execute polyphase-sort (dissolution) in order to adjust the interpolator. Both the interpolator and the decimeter form periodic time invariance systems, thus
10 having different characteristics from the time invariance system.

 Distortion so called as the chessboard distortion on lattice occurs in the resolution conversion of the picture caused by the periodic time invariance property
15 of the interpolator.

 Accordingly, Harada, and Takaie considered the condition for avoiding such chessboard distortion from the viewpoint of zero-point arrangement of filter (see, Yasuhiro Harada, Hitoshi Kiya,: "Multi-rate Filter
20 without Accompanying Chessboard Distortion and its Zero-point Arrangement" The technical Report of IEICE CAS96-78, pp1-6, 1997-01).

 Transfer function $H(z)$ for the multi-rate filter without accompanying the chessboard distortion will be
25 discussed. The transfer function $H(z)$ is capable of

being found in such a way as to multiply a transfer
 function $K(z)$ of the linear-phase FIR filter
 (hereinafter referred to as an equalizer) designed by a
 method in some kind by the transfer function $Z(z)$ of the
 5 zero-point in order to avoid the chessboard distortion
 later.

$$H(z) = Z(z) \cdot K(z) \quad (1)$$

10
$$Z(z) = 1 + z^{-1} + z^{-2} + \dots + z^{-(U-1)} \quad (2)$$

Here, a linear-phase FIR filter fixed beforehand
 such as the transfer function $Z(z)$ of the zero-point for
 avoiding the chessboard distortion is called as a pre-
 15 filter.

Fig.2 shows an example of a frequency response of
 the multi-rate filter and weighted approximation error,
 in which the chessboard distortion is avoided by
 multiplying the equalizer designed by the use of Remez
 20 Exchange algorithms and the pre-filter.

However, it suffers from the disadvantage in the
 avoiding method of the chessboard distortion according to
 the aforementioned method.

Namely, as illustrated in Fig. 2C, in the multi-
 25 rate filter having the transfer function $H(z)$ designed

depending on the conventional method, the equi-ripple of the weighted approximation error designed depending on the Remez Exchange algorithms is not established.

Further, as illustrated in Fig. 2B, the multi-rate filter designed depending on the conventional method, has gain of pass band with non-fixed value in which right end is attenuated.

If the resolution conversion is executed using such filter, contours of picture appears fuzzy, thus is adversely affected on quality of the picture.

The attenuation of this pass band can not be avoided even though the number of coefficient of filter is increased.

15 SUMMARY OF THE INVENTION

An object of the present invention is to provide an FIR filter and setting method of its coefficients in which the equi-ripple of the weighted approximation error is not established, and further it is possible to maintain a gain of the pass band at approximately constant value.

In order to achieve the above-mentioned objects, an FIR filter of the present invention has a configuration in which an impulse response is expressed by using a finite time length, this impulse response is equivalent

to a filter coefficient of the FIR filter, and the FIR filter's transfer function $H(z)$ is related to a transfer function $Z(z)$ of a pre-filter, wherein the filter coefficient is set by performing a weighted approximation to the desired characteristics in relation to the frequency response of the pre-filter.

Also, an FIR filter of the present invention has a configuration in which the FIR filter's impulse response is expressed by using a finite time length, this impulse response is equivalent to a filter coefficient of the FIR filter, and whose transfer function $H(z)$ is related to a transfer function $Z(z)$ of a pre-filter, and a transfer function $K(z)$ of an equalizer, wherein the filter coefficient is set on the basis of an amplitude characteristic of the equalizer that is obtained in such a way as to execute weighted approximation to the desired characteristics in relation to a frequency response of the pre-filter.

Also, a setting method of filter coefficients of an FIR filter of the present invention has a method in which the FIR filter's impulse response is expressed by using a finite time length, this impulse response is equivalent to a filter coefficient of the FIR filter, and whose transfer function $H(z)$ is related to a transfer function $Z(z)$ of a pre-filter, wherein the filter coefficient is

calculated by performing a weighted approximation to the desired characteristics in relation to a frequency response of the pre-filter.

Also, a setting method of filter coefficients of an
5 FIR filter of the present invention has a method in which the FIR filter's impulse response is expressed by using a finite time length, this impulse response is equivalent to a filter coefficient of the FIR filter, and whose transfer function $H(z)$ is related to a transfer function
10 $Z(z)$ of a pre-filter and a transfer function $K(z)$ of an equalizer, wherein the filter coefficient is calculated depending on an amplitude characteristic of the equalizer, which is obtained in such a way as to execute weighted approximation to the desired characteristics in
15 relation to a frequency response of the pre-filter.

Also, a setting method of filter coefficients of an FIR filter of the present invention has a method in which weighted approximation is executed to the desired characteristics by using the Remez Exchange algorithms
20 taking into account a frequency response of a pre-filter.

Also, a setting method of filter coefficients of an FIR filter of the present invention has a method in which the FIR filter's impulse response is expressed by a finite time length, and this impulse response is
25 equivalent to a filter coefficient, the setting method of

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a filter coefficient of the FIR filter comprises: a first step for generating an interpolation polynomial equation for interpolating an amplitude characteristic from an extreme value point of the amplitude characteristic of a frequency; a second step for determining a new extreme value point from the amplitude characteristic obtained from the interpolation polynomial equation that is generated in the first step; a third step for judging whether or not a position of the extreme value is approximated within required range by repeating the operation in the first step and the second step; and a fourth step for finding the filter coefficient from the approximated amplitude characteristic obtained in the third step.

15 Also, a setting method of filter coefficients of an FIR filter of the present invention has a method in which there is further provided an initial setting step for carrying out, at least, setting of the FIR filter, setting of the band, setting of coefficient of a pre-
20 filter, and setting of initial extreme value point, before executing the operation the first step.

Also, a setting method of filter coefficients of an FIR filter of the present invention has a method, in the second step and the third step, the extreme-value of,
25 weighted approximation error calculated from the extreme-

value point used for the interpolation is searched for the entire approximation band, then obtained extreme-value is taken to be a new extreme-value point, and it is judged that the optimum approximation is obtained when
 5 the position of the extreme-value is not changed.

Also, a setting method of filter coefficients of an FIR filter of the present invention has a method, in the fourth step, the filter coefficient is calculated by performing a weighted approximation to the desired
 10 characteristics in relation to a frequency response of the pre-filter.

Also, a setting method of filter coefficients of an FIR filter of the present invention has a method, in the fourth step, the filter coefficient is calculated
 15 depending on amplitude characteristic of the equalizer obtained in such a way as to execute weighted approximation to the desired characteristics in relation to a frequency response of the pre-filter.

Also, an FIR filter whose impulse response is
 20 expressed by using a finite time length, the impulse response being equivalent to a filter coefficient of the FIR filter, the FIR filter having arbitrary number of taps, and whose transfer function $H(z)$ is related to a transfer function $Z(z)$ of a pre-filter, wherein the
 25 filter coefficient is set in such a way as to perform a

weighted approximation to the desired characteristics so as to satisfy attenuation quantity of a stop band in relation to a frequency response of the pre-filter which satisfies the attenuation quantity of the stop band, when
 5 the number of taps is variable and the bandwidth is fixed.

Also, an FIR filter whose impulse response is expressed by using a finite time length, the impulse response being equivalent to a filter coefficient of the
 10 FIR filter, the FIR filter having arbitrary number of taps, and whose transfer function $H(z)$ is related to a transfer function $Z(z)$ of a pre-filter and transfer function $K(z)$ of an equalizer, wherein the filter coefficient is set on the basis of an amplitude
 15 characteristic of the equalizer obtained in such a way as to perform a weighted approximation to the desired characteristics so as to satisfy an attenuation quantity of a stop band in relation to frequency response of the pre-filter which satisfies the attenuation quantity of
 20 the stop band, when the number of taps is variable and the bandwidth is fixed.

Also, a setting method of filter coefficients of an FIR filter of the present invention has a method in which the FIR filter's impulse response is expressed by using a
 25 finite time length, this impulse response is equivalent

to a filter coefficient of the FIR filter, the FIR filter has arbitrary number of tap, and whose transfer function $H(z)$ is related to a transfer function $Z(z)$ of a pre-filter, wherein the filter coefficient is calculated by performing a weighted approximation to the desired characteristics so as to satisfy attenuation quantity of a stop band in relation to the frequency response of the pre-filter which satisfies attenuation quantity of the stop band, when band is made to fix and the number of tap is made variable.

Also, a setting method of filter coefficients of an FIR filter of the present invention has a method in which the FIR filter's impulse response is expressed by using a finite time length, this impulse response is equivalent to a filter coefficient of the FIR filter, the FIR filter has arbitrary number of tap, and whose transfer function $H(z)$ is related to a transfer function $Z(z)$ of a pre-filter and a transfer function $K(z)$ of an equalizer, wherein the filter coefficient is calculated depending on an amplitude characteristic of the equalizer obtained in such a way as to execute weighted approximation to the desired characteristics so as to satisfy attenuation quantity of a stop band in relation to the frequency response of the pre-filter which satisfies attenuation quantity of the stop band, when band is made to fix and

the number of tap is made variable.

Also, a setting method of filter coefficients of an FIR filter of the present invention has a method in which the FIR filter's impulse response is expressed by using a finite time length, this impulse response is equivalent to a filter coefficient of the FIR filter, and the FIR filter's number of tap is variable, and whose band is fixed, the setting method of a filter coefficient of an FIR filter comprises the steps of: a first step for generating interpolation polynomial equation for interpolating an amplitude characteristic from an extreme value point of the amplitude characteristic of the frequency; a second step for determining new extreme value point from the amplitude characteristic obtained from the interpolation polynomial equation that is obtained in the first step; a third step for judging whether or not position of the extreme value is approximated within required range while repeating the first step and the second step; a fourth step for examining attenuation quantity of a stop band from the approximated amplitude characteristic obtained in the third step; a fifth step for comparing the examined attenuation quantity with the attenuation quantity of the stop band thus designated to judge whether or not result of the comparison satisfies predetermined condition; a

sixth step for changing the number of tap when result of the comparison of the fifth step does not satisfy the predetermined condition; and a seventh step for finding the filter coefficient from the amplitude characteristic thus approximated depending on the third step which satisfies the predetermined condition in the fifth step.

Also a setting method of filter coefficients of an FIR filter of the present invention has a method, wherein there is provided at least an initial setting step for carrying out setting of the FIR filter, setting of the band, setting of coefficient of a pre-filter, and setting of initial extreme value point, before executing the first step.

Also, a setting method of filter coefficients of an FIR filter of the present invention has a method, in the fourth step, the minimum attenuation quantity in the stop band is examined, and in the sixth step, the number of the tap is increased.

Also, a setting method of filter coefficients of an FIR filter of the present invention has a method, in the above described seventh step, the filter coefficient is calculated by performing a weighted approximation with reference to the desired characteristics so as to satisfy attenuation quantity of a stop band in relation to frequency response of the pre-filter that satisfies the

attenuation quantity of the stop band when a band is fixed and the number of tap is made variable.

Also, a setting method of filter coefficients of an FIR filter of the present invention has a method, in the above described seventh step, the filter coefficient is calculated depending on an amplitude characteristic of an equalizer obtained in such a way as to execute weighted approximation with reference to the desired characteristics so as to satisfy attenuation quantity of a stop band in relation to frequency response of the pre-filter that satisfies the attenuation quantity of the stop band when a band is fixed and the number of tap is made variable.

Also, an FIR filter of the present invention has a configuration in which the FIR filter's impulse response is expressed by using a finite time length, this impulse response is equivalent to a filter coefficient of the FIR filter, the FIR filter has arbitrary number of tap, and whose transfer function $H(z)$ is related to a transfer function $Z(z)$ of a pre-filter, wherein the filter coefficient is set in such a way as to execute weighted approximation to the desired characteristics so as to satisfy attenuation quantity of a stop band in relation to frequency response of the pre-filter which satisfies attenuation quantity of a stop band, when the number of

taps is made to fix and band setting is changeable.

Also, an FIR filter of the present invention has a configuration in which the FIR filter's impulse response is expressed by using a finite time length, this impulse
 5 response is equivalent to a filter coefficient of the FIR filter, the FIR filter has arbitrary number of tap, and whose transfer function $H(z)$ is related to a transfer function $Z(z)$ of a pre-filter and transfer function $K(z)$ of an equalizer, wherein the filter coefficient is
 10 set on the basis of an amplitude characteristic of the equalizer obtained in such a way as to execute weighted approximation to the desired characteristics so as to satisfy attenuation quantity of a stop band in relation to frequency response of the pre-filter which satisfies
 15 attenuation quantity of a stop band, when the number of taps is made to fix and band setting is changeable.

Also, a setting method of filter coefficients of an FIR filter of the present invention has a method in which the FIR filter's impulse response is expressed by using a
 20 finite time length, this impulse response is equivalent to a filter coefficient of the FIR filter, the FIR filter has arbitrary number of tap, and whose transfer function $H(z)$ is related to a transfer function $Z(z)$ of a pre-filter, wherein the filter coefficient is calculated by
 25 performing a weighted approximation to the desired

characteristics so as to satisfy attenuation quantity of a stop band in relation to the frequency response of the pre-filter which satisfies attenuation quantity of the stop band, when the number of taps is made to fix and
 5 band setting is changeable.

Also, a setting method of filter coefficients of an FIR filter of the present invention has a method in which the FIR filter's impulse response is expressed by using a finite time length, this impulse response is equivalent
 10 to a filter coefficient of the FIR filter, the FIR filter has arbitrary number of tap, and whose transfer function $H(z)$ is related to a transfer function $Z(z)$ of a pre-filter and a transfer function $K(z)$ of an equalizer, wherein the filter coefficient is calculated depending on
 15 an amplitude characteristic of the equalizer obtained in such a way as to execute weighted approximation to the desired characteristics so as to satisfy attenuation quantity of a stop band in relation to the frequency response of the pre-filter which satisfies attenuation
 20 quantity of the stop band, when the number of taps is made to fix and band setting is changeable.

Also, a setting method of filter coefficients of an FIR filter of the present invention has a method in which the FIR filter's impulse response is expressed by using a
 25 finite time length, this impulse response is equivalent

to a filter coefficient of the FIR filter, and the FIR filter's number of tap is fixed, and whose band setting is changeable, the setting method of a filter coefficient of an FIR filter comprises the steps of: a first step for
5 generating interpolation polynomial equation for interpolating an amplitude characteristic from an extreme value point of the amplitude characteristic of the frequency; a second step for determining new extreme value point from the amplitude characteristic obtained
10 from the interpolation polynomial equation that is obtained in the first step; a third step for judging whether or not position of the extreme value is approximated within required range while repeating the first step and the second step; a fourth step for
15 examining attenuation quantity of a stop band from the approximated amplitude characteristic obtained in the third step; a fifth step for comparing the examined attenuation quantity with the attenuation quantity of the stop band thus designated to judge whether or not result
20 of the comparison satisfies predetermined condition; a sixth step for changing the band setting when result of the comparison of the fifth step does not satisfy the predetermined condition; and a seventh step for finding the filter coefficient from the amplitude characteristic
25 thus approximated depending on the third step which

satisfies the predetermined condition in the fifth step.

Also, a setting method of filter coefficients of an FIR filter of the present invention has a method, wherein there is provided an initial setting step for carrying
5 out, at least, setting of the FIR filter, setting of the band, setting of coefficient of a pre-filter, and setting of initial extreme value point, before executing the first step.

Also, a setting method of filter coefficients of an
10 FIR filter of the present invention has a method, in the fourth step, the minimum attenuation quantity in the stop band is examined.

Also, a setting method of filter coefficients of an FIR filter of the present invention, in the above
15 described seventh step, the filter coefficient is calculated by performing a weighted approximation with reference to the desired characteristics so as to satisfy attenuation quantity of a stop band in relation to frequency response of the pre-filter that satisfies the
20 attenuation quantity of the stop band when the number of taps is fixed and the band setting is changeable.

Also, a setting method of filter coefficients of an FIR filter of the present invention has a method, in the above described seventh step, the filter coefficient is
25 calculated depending on an amplitude characteristic of an

equalizer obtained in such a way as to execute weighted approximation with reference to the desired characteristics so as to satisfy attenuation quantity of a stop band in relation to frequency response of the pre-
5 filter that satisfies the attenuation quantity of the stop band when the number of taps is fixed and the band setting is changeable.

Also, an FIR filter of the present invention has a configuration in which the FIR filter's impulse response
10 is expressed by using a finite time length, this impulse response is equivalent to a filter coefficient of the FIR filter, the FIR filter has arbitrary number of tap, and whose transfer function $H(z)$ is related to a transfer function $Z(z)$ of a pre-filter, wherein the filter
15 coefficient is set in such a way as to execute weighted approximation to the desired characteristics so as to satisfy attenuation quantity of a stop band in relation to frequency response of the pre-filter which satisfies attenuation quantity of a stop band, when the number of
20 taps is variable and band setting is changeable.

Also, an FIR filter of the present invention has a configuration in which the FIR filter's impulse response is expressed by using a finite time length, this impulse response is equivalent to a filter coefficient of the FIR
25 filter, the FIR filter has arbitrary number of tap, and

whose transfer function $H(z)$ is related to a transfer function $Z(z)$ of a pre-filter and transfer function $K(z)$ of an equalizer, wherein the filter coefficient is set on the basis of an amplitude characteristic of the equalizer obtained in such a way as to execute weighted approximation to the desired characteristics so as to satisfy attenuation quantity of a stop band in relation to frequency response of the pre-filter which satisfies attenuation quantity of a stop band, when the number of taps is variable and band setting is changeable.

Also, a setting method of filter coefficients of an FIR filter of the present invention has a way in which the FIR filter's impulse response is expressed by using a finite time length, this impulse response is equivalent to a filter coefficient of the FIR filter, the FIR filter has arbitrary number of tap, and whose transfer function $H(z)$ is related to a transfer function $Z(z)$ of a pre-filter, wherein the filter coefficient is calculated by performing a weighted approximation to the desired characteristics so as to satisfy attenuation quantity of a stop band in relation to the frequency response of the pre-filter which satisfies attenuation quantity of the stop band, when the number of taps is variable and band setting is changeable.

Also, a setting method of filter coefficients of an

FIR filter of the present invention has a way in which
 the FIR filter's impulse response is expressed by using a
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 FIR filter of the present invention has a way in which
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 20 to a filter coefficient of the FIR filter, and the FIR
 filter's number of tap is variable, and whose band
 setting is changeable, the setting method of a filter
 coefficient of an FIR filter comprises the steps of: a
 first step for generating interpolation polynomial
 25 equation for interpolating an amplitude characteristic

from an extreme value point of the amplitude characteristic of the frequency; a second step for determining new extreme value point from the amplitude characteristic obtained from the interpolation polynomial equation that is obtained in the first step; a third step for judging whether or not position of the extreme value is approximated within required range while repeating the first step and the second step; a fourth step for examining attenuation quantity of a stop band from the approximated amplitude characteristic obtained in the third step; a fifth step for comparing the examined attenuation quantity with the attenuation quantity of the stop band thus designated to judge whether or not result of the comparison satisfies predetermined condition; a sixth step for changing the band setting when result of the comparison of the fifth step does not satisfy the predetermined condition; a seventh step for judging whether or not the present number of taps are capable of satisfying the attenuation quantity of the stop band after changing of the band in the sixth step; an eighth step for changing the number of taps when judgement is performed that the present number of taps do not satisfy the attenuation quantity of the stop band in the seventh step; and a ninth step for finding the filter coefficient from the amplitude characteristic thus approximated

depending on the third step which satisfies the predetermined condition in the fifth step.

Also, a setting method of filter coefficients of an FIR filter of the present invention has a way, wherein
5 there is provided at least an initial setting step for carrying out setting of the FIR filter, setting of the band, setting of coefficient of a pre-filter, and setting of initial extreme value point, before executing the first step.

10 Also, a setting method of filter coefficients of an FIR filter of the present invention has a way, in the fourth step, the minimum attenuation quantity in the stop band is examined, and in the eighth step, the number of the tap is increased.

15 Also, a setting method of filter coefficients of an FIR filter of the present invention has a way, in the above described ninth step, the filter coefficient is calculated by performing a weighted approximation with reference to the desired characteristics so as to satisfy
20 attenuation quantity of a stop band in relation to frequency response of the pre-filter that satisfies the attenuation quantity of the stop band when the number of taps is variable and band setting is changeable.

Also, a setting method of filter coefficients of an
25 FIR filter of the present invention has a way, in the

above described ninth step, the filter coefficient is calculated depending on an amplitude characteristic of an equalizer obtained in such a way as to execute weighted approximation with reference to the desired

5 characteristics so as to satisfy attenuation quantity of a stop band in relation to frequency response of the pre-filter that satisfies the attenuation quantity of the stop band when the number of taps is variable and the band setting is changeable.

10 Also, an FIR filter of the present invention has a configuration in which the FIR filter's impulse response is expressed by using a finite time length, this impulse response is equivalent to a filter coefficient of the FIR filter, the FIR filter has arbitrary number of tap, and
15 whose transfer function $H(z)$ is related to a transfer function $Z(z)$ of a pre-filter, wherein the filter coefficient is set in such a way as to execute weighted approximation to the desired characteristics so as to satisfy attenuation quantity of a stop band in relation
20 to frequency response of the pre-filter through which the attenuation quantity of the designated frequency of a transition band is passed, and which satisfies attenuation quantity of a stop band, when the number of taps is made to fix and band setting is changeable.

25 Also, an FIR filter of the present invention has a

configuration in which the FIR filter's impulse response is expressed by using a finite time length, this impulse response is equivalent to a filter coefficient of the FIR filter, the FIR filter has arbitrary number of tap, and
5 whose transfer function $H(z)$ is related to a transfer function $Z(z)$ of a pre-filter and transfer function $K(z)$ of an equalizer, wherein the filter coefficient is set on the basis of an amplitude characteristic of the equalizer obtained in such a way as to execute weighted
10 approximation to the desired characteristics so as to satisfy attenuation quantity of a stop band in relation to frequency response of the pre-filter through which the attenuation quantity of the designated frequency of a transition band is passed, and which satisfies
15 attenuation quantity of a stop band, when the number of taps is made to fix and band setting is changeable.

Also, a setting method of filter coefficients of an FIR filter of the present invention has a way in which the FIR filter's impulse response is expressed by using a
20 finite time length, this impulse response is equivalent to a filter coefficient of the FIR filter, the FIR filter has arbitrary number of tap, and whose transfer function $H(z)$ is related to a transfer function $Z(z)$ of a pre-filter, wherein the filter coefficient is calculated by
25 performing a weighted approximation to the desired

characteristics so as to satisfy attenuation quantity of a stop band in relation to the frequency response of the pre-filter through which attenuation quantity of the designated frequency of a stop band is passed, and which
5 satisfies attenuation quantity of the stop band, when the number of taps is made to fix and band setting is changeable.

Also, a setting method of filter coefficients of an FIR filter of the present invention has a way in which
10 the FIR filter's impulse response is expressed by using a finite time length, this impulse response is equivalent to a filter coefficient of the FIR filter, the FIR filter has arbitrary number of tap, and whose transfer function $H(z)$ is related to a transfer function $Z(z)$ of a pre-
15 filter and a transfer function $K(z)$ of an equalizer, wherein the filter coefficient is calculated depending on an amplitude characteristic of the equalizer obtained in such a way as to execute weighted approximation to the desired characteristics so as to satisfy attenuation
20 quantity of a stop band in relation to the frequency response of the pre-filter through which attenuation quantity of the designated frequency of a stop band is passed, and which satisfies attenuation quantity of the stop band, when the number of taps is made to fix and
25 band setting is changeable.

Also, a setting method of filter coefficients of an FIR filter of the present invention has a way in which the FIR filter's impulse response is expressed by using a finite time length, this impulse response is equivalent to a filter coefficient of the FIR filter, and the FIR filter's number of tap is fixed, and whose band setting is changeable, the setting method of a filter coefficient of an FIR filter comprises the steps of: a first step for generating interpolation polynomial equation for
10 interpolating an amplitude characteristic from an extreme value point of the amplitude characteristic of the frequency; a second step for determining new extreme value point from the amplitude characteristic obtained from the interpolation polynomial equation that is
15 obtained in the first step; a third step for judging whether or not position of the extreme value is approximated within required range while repeating the first step and the second step; a fourth step for examining attenuation quantity of a stop band from the approximated amplitude characteristic obtained in the
20 third step; a fifth step for comparing the examined attenuation quantity in the fourth step with the attenuation quantity of the stop band thus designated to judge whether or not result of the comparison satisfies
25 predetermined condition; a sixth step for changing the

band setting when result of the comparison of the fifth
step does not satisfy the predetermined condition; a
seventh step for examining attenuation quantity of the
designated frequency of the transition band which
5 attenuation quantity satisfies predetermined condition in
the fifth step; an eighth step for comparing the
attenuation quantity of the designated frequency of the
transition band that is examined in the seventh step with
the attenuation quantity of the designated transition
10 band, and for judging whether or not result of comparison
satisfies predetermined condition; a ninth step for
changing setting of the band when result of comparison of
the seventh step does not satisfy the predetermined
condition; and a tenth step for finding the filter
15 coefficient from the amplitude characteristic thus
approximated depending on the seventh step which
amplitude characteristic satisfies the predetermined
condition.

Also, a setting method of filter coefficients of an
20 FIR filter of the present invention has a way, wherein
there is provided at least an initial setting step for
carrying out setting of the FIR filter, setting of the
band, setting of coefficient of a pre-filter, and setting
of initial extreme value point, before executing the
25 first step.

Also, a setting method of filter coefficients of an FIR filter of the present invention has a way, in the fourth step, the minimum attenuation quantity in the stop band is examined.

5 Also, a setting method of filter coefficients of an FIR filter of the present invention has a way, in the above described tenth step, the filter coefficient is calculated by performing a weighted approximation with reference to the desired characteristics so as to satisfy
10 attenuation quantity of a stop band in relation to frequency response of the pre-filter that satisfies the attenuation quantity of the stop band, and that causes the attenuation quantity of the designated frequency of the transition band to pass when the number of taps is
15 fixed and band setting is changeable.

Also, a setting method of filter coefficients of an FIR filter of the present invention has a way, in the above described tenth step, the filter coefficient is calculated depending on an amplitude characteristic of an
20 equalizer obtained in such a way as to execute weighted approximation with reference to the desired characteristics so as to satisfy attenuation quantity of a stop band in relation to frequency response of the pre-filter that satisfies the attenuation quantity of the
25 stop band, and that causes the attenuation quantity of

the designated frequency of the transition band to pass when the number of taps is fixed and the band setting is changeable.

Also, an FIR filter of the present invention has a
5 configuration in which the FIR filter's impulse response is expressed by using a finite time length, this impulse response is equivalent to a filter coefficient of the FIR filter, the FIR filter has arbitrary number of tap, and whose transfer function $H(z)$ is related to a transfer
10 function $Z(z)$ of a pre-filter, wherein the filter coefficient is set in such a way as to execute weighted approximation to the desired characteristics so as to satisfy attenuation quantity of a stop band in relation to frequency response of the pre-filter through which the
15 attenuation quantity of the designated frequency of a transition band is passed, and which satisfies attenuation quantity of a stop band, when the number of taps is variable and band setting is changeable.

Also, an FIR filter of the present invention has a
20 configuration in which the FIR filter's impulse response is expressed by using a finite time length, this impulse response is equivalent to a filter coefficient of the FIR filter, the FIR filter has arbitrary number of tap, and whose transfer function $H(z)$ is related to a transfer
25 function $Z(z)$ of a pre-filter and transfer function K

(z) of an equalizer, wherein the filter coefficient is set on the basis of an amplitude characteristic of the equalizer obtained in such a way as to execute weighted approximation to the desired characteristics so as to satisfy attenuation quantity of a stop band in relation to frequency response of the pre-filter through which the attenuation quantity of the designated frequency of a transition band is passed, and which satisfies attenuation quantity of a stop band, when the number of taps is variable and band setting is changeable.

Also, a setting method of filter coefficients of an FIR filter of the present invention has a way in which the FIR filter's impulse response is expressed by using a finite time length, this impulse response is equivalent to a filter coefficient of the FIR filter, the FIR filter has arbitrary number of tap, and whose transfer function $H(z)$ is related to a transfer function $Z(z)$ of a pre-filter, wherein the filter coefficient is calculated by performing a weighted approximation to the desired characteristics so as to satisfy attenuation quantity of a stop band in relation to the frequency response of the pre-filter through which attenuation quantity of the designated frequency of a stop band is passed, and which satisfies attenuation quantity of the stop band, when the number of taps variable and band setting is changeable.

Also, a setting method of filter coefficients of an FIR filter of the present invention has a way in which the FIR filter's impulse response is expressed by using a finite time length, this impulse response is equivalent to a filter coefficient of the FIR filter, the FIR filter has arbitrary number of tap, and whose transfer function $H(z)$ is related to a transfer function $Z(z)$ of a pre-filter and a transfer function $K(z)$ of an equalizer, wherein the filter coefficient is calculated depending on an amplitude characteristic of the equalizer obtained in such a way as to execute weighted approximation to the desired characteristics so as to satisfy attenuation quantity of a stop band in relation to the frequency response of the pre-filter through which attenuation quantity of the designated frequency of a stop band is passed, and which satisfies attenuation quantity of the stop band, when the number of taps is variable and band setting is changeable.

Also, a setting method of filter coefficients of an FIR filter of the present invention has a way in which the FIR filter's impulse response is expressed by using a finite time length, this impulse response is equivalent to a filter coefficient of the FIR filter, and the FIR filter's number of tap is variable, and whose band setting is changeable, the setting method of a filter

coefficient of an FIR filter comprises the steps of: a first step for generating interpolation polynomial equation for interpolating an amplitude characteristic from an extreme value point of the amplitude characteristic of the frequency; a second step for determining new extreme value point from the amplitude characteristic obtained from the interpolation polynomial equation that is obtained in the first step; a third step for judging whether or not position of the extreme value is approximated within required range while repeating the first step and the second step; a fourth step for examining attenuation quantity of a stop band from the approximated amplitude characteristic obtained in the third step; a fifth step for comparing the examined attenuation quantity in the fourth step with the attenuation quantity of the stop band thus designated to judge whether or not result of the comparison satisfies predetermined condition; a sixth step for changing the band setting when result of the comparison of the fifth step does not satisfy the predetermined condition; a seventh step for judging whether or not the present number of taps is capable of satisfying attenuation quantity of a stop band after changing of the band in the sixth step; an eighth step for changing the number of taps when judgement is performed that the present number

of taps can not satisfy the attenuation quantity in the seventh step; a ninth step for examining attenuation quantity of the designated frequency of the transition band which attenuation quantity satisfies predetermined condition in the fifth step; a tenth step for comparing the attenuation quantity of the designated frequency of the transition band that is examined in the ninth step with the attenuation quantity of the designated transition band, and for judging whether or not result of comparison satisfies predetermined condition; an eleventh step for changing setting of the band when result of comparison of the tenth step does not satisfy the predetermined condition; a twelfth step for judging whether or not the present number of taps causes the signal to pass the designated frequency of the stop band after changing the band in the eleventh step; a thirteenth step changing the number of taps when judgement is performed that the present number of taps does not enable the designated frequency to be passed in the twelfth step; and a fourteenth step for finding the filter coefficient from the amplitude characteristic thus approximated depending on the tenth step which amplitude characteristic satisfies the predetermined condition.

Also, a setting method of filter coefficients of an FIR filter of the present invention has a way, wherein

there is provided at least an initial setting step for carrying out setting of the FIR filter, setting of the band, setting of coefficient of a pre-filter, and setting of initial extreme value point, before executing the
5 first step.

Also, a setting method of filter coefficients of an FIR filter of the present invention has a way, in the fourth step, the minimum attenuation quantity in the stop band is examined, and both in the eighth step and in the
10 thirteenth step, the number of the tap is increased.

Also, a setting method of filter coefficients of an FIR filter of the present invention has a way, in the above described fourteenth step, the filter coefficient is calculated by performing a weighted approximation with
15 reference to the desired characteristics so as to satisfy attenuation quantity of a stop band in relation to frequency response of the pre-filter that satisfies the attenuation quantity of the stop band, and that causes the attenuation quantity of the designated frequency of
20 the transition band to pass when the number of taps is variable and band setting is changeable.

Also, a setting method of filter coefficients of an FIR filter of the present invention has a way, in the above described fourteenth step, the filter coefficient
25 is calculated depending on an amplitude characteristic of

an equalizer obtained in such a way as to execute weighted approximation with reference to the desired characteristics so as to satisfy attenuation quantity of a stop band in relation to frequency response of the pre-
5 filter that satisfies the attenuation quantity of the stop band, and that causes the attenuation quantity of the designated frequency of the transition band to pass when the number of taps is variable and the band setting is changeable.

10 According to the present invention, for instance, depending on the initial setting, the setting of the linear-phase FIR filter, the setting of the band, the setting of the coefficient of the pre-filter, and the setting of the extreme-value point are carried out.

15 Subsequently, an interpolation polynomial equation is generated for interpolating amplitude characteristic from the present extreme value point of the amplitude characteristic of the frequency.

Next, a new extreme value point is determined from
20 the amplitude characteristic obtained from the interpolation polynomial equation that is obtained in the first step.

Judgement is performed whether or not position of the extreme value is approximated within required range while
25 repeating the first step and the second step.

Then, finding of the filter coefficient is performed from the approximated amplitude characteristic obtained.

Thus, the FIR filter whose coefficient is set, is capable of possessing the weighted approximation error
 5 with equi-ripple, further in which gain of the pass band is maintained constant value.

BRIEF DESCRIPTION OF THE DRAWINGS

These and other objects and features of the present
 10 invention will become clearer from the following description of the preferred embodiments with reference to the accompanying drawings, in which:

Fig. 1 is a view illustrating a transversal type circuit configuration of an FIR filter;

15 Figs.2A to 2C are views illustrating one example of frequency response and weighted approximation error in order to avoid the chessboard distortion in the conventional method;

Figs.3A to 3D are views illustrating impulse response
 20 of four cases where the FIR filter possesses linear-phase;

Fig.4 is a view illustrating $Q(e^{j\omega})$ and R to four cases of the linear-phase FIR filter;

Fig.5 is a view illustrating example of weighted
 25 Chebyshev approximation;

Fig.6 is a flowchart of the Remez Exchange algorithms while taking into account frequency response of the pre-filter according to the present invention;

Figs.7A to 7C are views for explaining determining
 5 method of new extreme value of the weighted approximation error $E(e^{j\omega})$;

Fig.8 is a view illustrating frequency response of low-pass filter which avoids the chessboard distortion designed according to the present invention;

10 Figs.9A and 9B are views for comparing the frequency response of the low-pass filter designed by the conventional technique with the present invention respectively;

Fig.10 is a view illustrating weighted approximation
 15 error to the filter designed according to the present invention;

Fig.11 is a view illustrating flowchart of algorithms for finding filter which satisfies attenuation quantity of the stop band;

20 Fig.12 is a view illustrating parameter of algorithms for finding filter that satisfies the attenuation quantity of the stop band and has the maximum end frequency of the pass band;

Fig.13 is a view illustrating initial frequency of
 25 the dichotomizing method in the algorithms for finding

filter having the maximum end frequency of the pass band
which filter satisfies the attenuation quantity of the
stop band;

Figs.14A to 14C are views illustrating change of band
5 setting in loop of the first time;

Figs.15A and 15B are views illustrating change of
band setting in loop after the second time and later;

Fig.16 is a view illustrating frequency response of
the filter having the maximum end frequency of pass band
10 which filter satisfies attenuation quantity of the stop
band;

Fig.17 is a view illustrating parameter in the
algorithms for finding filter having the minimum starting
frequency of the stop band which filter satisfies
15 attenuation quantity of the stop band;

Fig.18 is a view illustrating initial frequency of
the dichotomizing method in the algorithms for finding
filter having the minimum starting frequency of the pass
band which filter satisfies the attenuation quantity of
20 the stop band;

Figs.19A to 19C are views illustrating change of band
setting in loop of the first time;

Figs.20A and 20B are views illustrating change of
band setting in loop after the second time and later;

25 Fig.21 is a view illustrating frequency response of

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the filter having the minimum starting frequency of stop band which filter satisfies attenuation quantity of the stop band;

Fig.22 is a view illustrating flowchart of the
5 algorithms for finding filter with the minimum number of tap that satisfies attenuation quantity of the stop band;

Fig.23 is a view illustrating frequency response of the filter with the minimum number of tap that satisfies attenuation quantity of the stop band;

10 Fig.24 is a view illustrating a flowchart of the algorithms for finding filter that satisfies the attenuation quantity of the stop band and that enable the signal to be passed through the frequency point of the transition band;

15 Fig.25 is a view illustrating algorithms (1) for finding filter that satisfies the attenuation quantity of the stop band and that enable the signal to be passed through the frequency point of the transition band;

Fig.26 is a view illustrating initial frequency of
20 the dichotomizing method in the algorithms for finding filter that satisfies the attenuation quantity of the stop band and that enables the signal to be passed through the frequency point of the transition band;

Figs.27A to 29C are views illustrating change of band
25 setting in loop of the first time;

Figs.28A and 28B are views illustrating change of band setting in loop after the second time and later;

Fig.29 is a view illustrating frequency response (1) of the filter that satisfies the attenuation quantity of the stop band and that enables the signal to be passed through the frequency point of the transition band;

Fig.30 is a view illustrating algorithms (2) for finding filter that satisfies the attenuation quantity of the stop band and that enable the signal to be passed through the frequency point of the transition band;

Fig.31 is a view illustrating initial frequency of the dichotomizing method in the algorithms for finding filter that satisfies the attenuation quantity of the stop band and that enables the signal to be passed through the frequency point of the transition band;

Figs.32A to 32C are views illustrating change of band setting in loop of the first time;

Figs.33A and 33B are views illustrating change of band setting in loop after the second time and later;

20 Fig.34 is a view illustrating frequency response (2)
of the filter that satisfies the attenuation quantity of
the stop band and that enables the signal to be passed
through the frequency point of the transition band;

Fig.35 is a view illustrating flowchart of the
25 algorithms for finding filter with the minimum number of

tap that satisfies attenuation quantity of the stop band;

Fig.36 is a view illustrating frequency response of the filter with the minimum number of tap that satisfies attenuation quantity of the stop band;

5 Fig.37 is a view illustrating frequency response of the filter with the minimum number of tap that satisfies attenuation quantity of the stop band;

Fig.38 is a view illustrating flowchart of the algorithms for finding filter with the minimum number of
10 tap that satisfies the attenuation quantity of the stop band and that enables the signal to be passed through the frequency band of the transition band; and

Fig.39 is a diagram illustrating frequency response of the filter with the minimum number of taps which
15 filter satisfies the attenuation quantity of the stop band, and which filter enables the signal to be passed through the frequency point of the transition band.

DESCRIPTION OF THE PREFERRED EMBODIMENTS

20 Below, preferred embodiments will be described with reference to the accompanying drawings.

Preferred embodiments of the present invention will be explained with reference to the accompanying drawings below.

25 A linear-phase FIR filter according to the present

invention is capable of equivalently adopting transversal type circuit configuration as illustrated in Fig.1. The FIR filter includes $n-1$ series-connected unit time delay elements 2-1 to 2- $n-1$, n multipliers 3-1 to 3- n having
 5 filter coefficients $h(0)$ to $h(n-1)$, where $(n-1)$ multipliers 3-1 to 3- $n-1$ are connected to input terminals of the corresponding unit time delay elements 2-1 to 2- $n-1$ and n -th multiplier 3- n is connected to an output terminal of n -th time unit time delay element 2- $n-1$, and
 10 an adder 4 connected to output terminals of the n multipliers 3-1 to 3- n . However, filter coefficients h , as described later in detail, can be obtained in such a way wherein the Remez Exchange algorithm is extended, and the desired amplitude characteristic is subjected to
 15 Chebyshev approximation under taking into account a frequency response of a pre-filter, and the filter coefficients h are obtained from the approximated amplitude characteristics.

Below, a concrete method for setting coefficients of
 20 the linear-phase FIR filter according to the present invention will be explained successively with reference to the drawings.

In equation (3), the transfer function $H(z)$ of the linear-phase FIR filter having N -tap is defined as a
 25 filter which calculates the product of the transfer

function $Z(z)$ of the pre-filter and the transfer function of the equalizer.

$$H(z) = Z(z) \cdot K(z) \quad \dots (3)$$

5

Here, the pre-filter is a U tap of the linear-phase FIR filter, and the equalizer is a $N - (U - 1)$ tap linear-phase FIR filter respectively. The transfer function of the pre-filter is previously given.

10 A design of a filter of the transfer function $H(z)$ is the determination of the transfer function $K(z)$ of the equalizer having $N - (U - 1)$ taps such that the amplitude characteristic $H(e^{j\omega})$ is approached to the desired amplitude characteristic $D(e^{j\omega})$.

15 In the present embodiment, in order to design the transfer function $H(z)$ under consideration of the amplitude characteristic $K(e^{j\omega})$ of such the pre-filter, a method in which the Remez Exchange algorithms is extended for solving Chebyshev approximation problem, is
20 adopted.

The number of taps allocated to the equalizer of the transfer function $K(z)$ is defined as $L = N - (U - 1)$.

The transfer function $K(z)$ of the linear-phase FIR filter, as illustrated in Figs. 3A to 3D, is categorized
25 with four cases because the transfer function thereof has

linear-phase.

Concretely, it is categorized into four cases, case 1 : odd number of taps, and even symmetry as illustrated in Fig.3A, case 2 : even number of taps, and even symmetry as illustrated in Fig.3B, case 3 : odd number of taps, and odd symmetry as illustrated in Fig.3C, and case 4 : even number of taps, and odd symmetry.

With reference to the case 1, the amplitude characteristic function $K(e^{j\omega})$ is made to leave as it is, and for the other cases 2 to 4, rewrite as follows.

$$\text{Case 1 : } \sum_{n=0}^{(L-1)/2} a(n) \cos(n\omega) \quad (4-1)$$

$$\begin{aligned} \text{Case 2 : } & \sum_{n=1}^{L/2} b(n) \cos\left\{\left(n - \frac{1}{2}\right)\omega\right\} \\ & = \cos\left(\frac{\omega}{2}\right) \sum_{n=0}^{L/2-1} \tilde{b}(n) \cos(n\omega) \end{aligned} \quad (4-2)$$

$$\begin{aligned} \text{Case 3 : } & \sum_{n=1}^{(L-1)/2} c(n) \sin(n\omega) \\ & = \sin(\omega) \sum_{n=0}^{(L-3)/2} \tilde{c}(n) \cos(n\omega) \end{aligned} \quad (4-3)$$

$$\begin{aligned} \text{Case 4 : } & \sum_{n=1}^{L/2} d(n) \sin\left\{\left(n - \frac{1}{2}\right)\omega\right\} \\ & = \sin\left(\frac{\omega}{2}\right) \sum_{n=0}^{L/2-1} \tilde{d}(n) \cos(n\omega) \end{aligned} \quad (4-4)$$

Namely, the amplitude characteristic function $K(e^{j\omega})$ is expressed by the product of the function $Q(e^{j\omega})$ of the fixed parameters as illustrated in Fig.4 and a cosine series $P(e^{j\omega})$ including the design parameters. Hereinafter, the upper limit of sum of the respective equations (4-1) to (4-4) is expressed as $R - 1$. Namely, R is calculated as shown in Fig.4.

Further, $a(n), \tilde{b}(n), \tilde{c}(n), \tilde{d}(n)$ are expressed generally as $P(n)$.

When the desired amplitude characteristic is taken to be $D(e^{j\omega})$, and weight to respective frequencies are taken to be $W(e^{j\omega})$, the weighted approximation error is defined as follows:

$$E(e^{j\omega}) = W(e^{j\omega}) \{ D(e^{j\omega}) - H(e^{j\omega}) \} \quad (5)$$

$$H(e^{j\omega}) = K(e^{j\omega}) \cdot Z(e^{j\omega}) = Q(e^{j\omega}) \cdot P(e^{j\omega}) \cdot Z(e^{j\omega}) \quad (6)$$

Substitute equation (6) into equation (5), the following equation is obtained.

$$E(e^{j\omega}) = \hat{W}(e^{j\omega}) \{ \hat{D}(e^{j\omega}) - P(e^{j\omega}) \} \quad (7)$$

However, $\hat{W}(e^{j\omega})$, $\hat{D}(e^{j\omega})$ are expressed as follows:

$$\hat{W}(e^{j\omega}) = W(e^{j\omega}) \cdot Q(e^{j\omega}) \cdot Z(e^{j\omega}) \quad (8)$$

$$\hat{D}(e^{j\omega}) = \frac{D(e^{j\omega})}{Q(e^{j\omega}) \cdot Z(e^{j\omega})} \quad (9)$$

The equation (7) expresses the weighted approximation error of the linear-phase FIR filter in the four cases of case 1 to case 4.

The weighted Chebyshev approximation problem is to determine $a(n), \hat{b}(n), \hat{c}(n), \hat{d}(n)$ of the equations (4-1) to (4-4) that makes to bring the maximum value of $|E(e^{j\omega})|$ within designated frequency band into minimum, in the equation (5).

Hereinafter, there will be explained in relation to the concrete example.

Here, the amplitude characteristic $D(e^{j\omega})$ is defined as illustrated in Fig.5 and the following.

$$\begin{aligned} D(e^{j\omega}) &= 1 \quad (\text{error within } \pm\delta_1, 0 < \omega < \omega_p) \\ D(e^{j\omega}) &= 0 \quad (\text{error within } \pm\delta_2, \omega_s < \omega < \pi) \end{aligned} \quad (10)$$

Note, when R is given, values of δ_1, δ_2 can not be designated arbitrarily, but it is possible to designate its ratio.

The $W(e^{j\omega})$ is taken to be a constant value W_1 in the pass band, and to be W_2 in the stop band, thus being selected in such a way that $W_1 \delta_1 = W_2 \delta_2$ stands. For instance, $W_1 = 1, W_2 = \delta_1 / \delta_2$ are made to select. At this time, next alternating theorem stands.

Theorem

The necessary and sufficient condition in order that the cosine series $P(e^{j\omega})$ of $(R - 1)$ order is the best weighted Chebyshev approximation to the target characteristic within the section $(0, \pi)$ of ω is as follows:

(1) $E(e^{j\omega})$ obtains the extreme value at least $(R + 1)$ times within the section $(0, \pi)$. At this time, frequency within which the extreme value is obtained is taken to be $\omega_0 < \omega_1 < \omega_2 < \dots < \omega_{(R-1)} < \omega_R$.

(2) The sign of the neighboring extreme values are different, and the absolute values of the whole extreme values are the same. Namely, the following conditions are satisfied.

$$E(e^{j\omega_i}) \cdot E(e^{j\omega_{i+1}}) < 0 \quad (i = 0, 1, \dots, R - 1)$$

$$|E(e^{j\omega i})| = |E(e^{j\omega i + \pi})| \quad (i = 0, 1, \dots, R - 1) \quad (11)$$

Consequently, $|E(e^{j\omega i})|$ is equal to the maximum value of $|E(e^{j\omega})|$ within the section.

- 5 There is known Remez Exchange algorithms on the basis of the alternating theorem as the technique for obtaining the best Chebyshev approximation (Rabiner, L.R., McClellan, J.H. and Parks, T.W.: "FIR Digital Filter Design Techniques Using Weighted Chebyshev Approximation", Proc. IEEE, Vol 63, April, pp.595-610, 10 1975).

15 The Remez Exchange algorithms is an algorithms in which the desired amplitude characteristic is carried out Chebyshev approximation within frequency domain, and coefficients of the linear-phase FIR filter is obtained from the resultant approximated amplitude characteristic.

Fig.6 is a flowchart of the Remez Exchange algorithms while taking into account a frequency response of the pre-filter according to the present invention.

- 20 The Remez Exchange algorithms while taking into account the concrete frequency response of the pre-filter is as follows:

Step 0

As illustrated in Fig.6, firstly, an initial setting

is executed (F 101). In this initial setting, setting of the linear-phase FIR filter, setting of a band, setting of a coefficient of the pre-filter, and setting of an initial extreme point are carried out.

5 Items set concretely are as follows:

- the number of tap,
- even symmetry or odd symmetry of the linear-phase FIR filter,
- the number of the band,
- 10 · the frequency of both ends of the respective bands,
- the desired amplitude value of the respective bands,
- weighting to the respective bands,
- coefficient of the pre-filter,
- 15 · the frequency $\omega^{(0)} = \omega_k^{(0)}$ ($k = 0, \dots, R$) that becomes the extreme value in the approximation band.

Note, the letter of right shoulder (i) expresses the number of repetition.

Step 1

20 Next, LaGrange's interpolation polynomial equation is generated for interpolating an amplitude characteristic from the current extreme value point (F 102).

Above equation (5) indicates the target function of the Chebyshev approximation. The necessary and sufficient
25 condition for obtaining the minimum value of the target

function of the Chebyshev approximation is indicated by the alternating theorem. Accordingly, parameter $p(n)$ of the following equation is found in such a way that, on the basis of the alternating theorem, the weighted approximation error $\delta^{(i)}$ from the desired amplitude characteristic at the respective frequency points are of equal, and sign is alternated.

$$P(e^{j\omega}) = \sum_{n=0}^{R-1} p(n) \cos(n\omega) \quad (12)$$

Namely, the weighted approximation error of the equation (7) at the frequency points $\omega^{(i)} = \omega_k^{(i)}$ ($k = 0, \dots, R$) satisfies the following equation.

$$\hat{W}(e^{j\omega_k^{(i)}}) \left\{ \hat{D}(e^{j\omega_k^{(i)}}) - P(e^{j\omega_k^{(i)}}) \right\} = (-1)^k \delta^{(i)} \quad (k=0,1,\dots,R) \quad (13)$$

Hereinafter, the right shoulder letter (i) is omitted for simplification. The equation (13) is carried as follows.

$$P(e^{j\omega_k}) + \frac{(-1)^k \delta}{\hat{W}(e^{j\omega_k})} = \hat{D}(e^{j\omega_k})$$

$$\sum_{n=0}^{R-1} p(n) \cos(n\omega_k) + \frac{(-1)^k \delta}{\hat{W}(e^{j\omega_k})} = \hat{D}(e^{j\omega_k}) \quad (k=0,1,\dots,R) \quad (14)$$

Matrix expression of the equation (14) is as follows:

$$\begin{bmatrix} 1 & \cos(\omega_0) & \cos(2\omega_0) & \cdots & \cos((R-1)\omega_0) & \frac{1}{\hat{W}(e^{j\omega_0})} \\ 1 & \cos(\omega_1) & \cos(2\omega_1) & \cdots & \cos((R-1)\omega_1) & \frac{-1}{\hat{W}(e^{j\omega_1})} \\ \vdots & \vdots & \vdots & \ddots & \vdots & \vdots \\ 1 & \cos(\omega_{R-1}) & \cos(2\omega_{R-1}) & \cdots & \cos((R-1)\omega_{R-1}) & \frac{(-1)^{R-1}}{\hat{W}(e^{j\omega_{R-1}})} \\ 1 & \cos(\omega_R) & \cos(2\omega_R) & \cdots & \cos((R-1)\omega_R) & \frac{(-1)^R}{\hat{W}(e^{j\omega_R})} \end{bmatrix} \begin{bmatrix} \rho(0) \\ \rho(1) \\ \vdots \\ \rho(R-1) \\ \delta \end{bmatrix} \quad (15)$$

$$= \begin{bmatrix} \hat{D}(e^{j\omega_0}) \\ \hat{D}(e^{j\omega_1}) \\ \vdots \\ \hat{D}(e^{j\omega_{R-1}}) \\ \hat{D}(e^{j\omega_R}) \end{bmatrix}$$

5 However, there are lot of amount of calculation for calculating this equation (15), accordingly, δ is analytically found firstly.

$$\delta = \frac{\sum_{j=0}^R \alpha_j D(e^{j\omega_j})}{\sum_{j=1}^R (-1)^j \alpha_j / \hat{W}(e^{j\omega_j})} \quad (16)$$

$$10 \quad \alpha_k = \prod_{\substack{j=1 \\ j \neq k}}^R \frac{1}{(X_k - X_j)} \quad (17)$$

$$X_j = \cos(\omega_j) \quad (18)$$

This α_k is surplus factor of component of k-column (R + 1)-row of the matrix F. Note, $\hat{W}(e^{j\omega})$ and $\hat{D}(e^{j\omega})$ use the equation (8) and the equation (9).

Next, the following equation is provided by using δ .

$$5 \quad C_k = \hat{D}(e^{j\omega_k}) - (-1)^k \frac{\delta}{\hat{W}(e^{j\omega_k})} \quad (k=0, \dots, R-1) \quad (19)$$

In order to find the amplitude characteristic of the frequency except for the extreme value point, the LaGrange's interpolation polynomial expression is used as
 10 an interpolation polynomial expression for interpolating using the extreme value point. Namely, $P(e^{j\omega})$ is calculated in such a way that the interpolation is executed so as to obtain value C_k at ω_k ($k=0, \dots, R-1$) by using the LaGrange's interpolation polynomial
 15 expression.

$$P(e^{j\omega}) = \frac{\sum_{k=0}^{R-1} C_k \left(\frac{\beta_k}{x - x_k} \right)}{\sum_{k=0}^{R-1} \left(\frac{\beta_k}{x - x_k} \right)} \quad (20)$$

$$\beta_k = \prod_{\substack{j=0 \\ j \neq k}}^{R-1} \frac{1}{(x - x_j)} \quad (21)$$

$$20 \quad x = \cos(\omega) \quad (22)$$

This result means the answer of the equation (15), and satisfies the equation (13) automatically at the point of ω_r .

Step 2

5 The new extreme value point is determined from the amplitude characteristic obtained from the interpolation polynomial expression (F 103), before returning to processing of F 102. Judgement is executed repeatedly whether or not the optimum approximation is obtained
10 after position of the extreme value is not changed (F 104).

Above described each extreme value point ω_k as a result of Step 1 is not necessarily the extreme value of the weighted function $E(e^{j\omega})$, in some cases, the point
15 which becomes $|E(e^{j\omega})| > \delta^{(i)}$ exists. Thus, the new extreme value $\omega^{(i+1)}$ is determined from the all point simultaneous replacement method.

All Point Simultaneous Replacement Method

On the basis of the following equation, the extreme
20 value of weighted approximation error calculated from the extreme value used for the interpolation is searched over the whole approximation bands, the searched extreme values are taken to be the new extreme values

$$\omega^{(i+1)} = \omega_k^{(i+1)} \quad (k = 0, 1, \dots, R), \text{ thus returning to Step}$$

1.

$$E(e^{j\omega}) = \hat{W}(e^{j\omega}) \{ \hat{D}(e^{j\omega}) - P(e^{j\omega}) \} \quad (23)$$

5 It is decided that when the position of the extreme value has not been changed, the optimum approximation is obtained. This is the condition of the termination of the repetition, when the condition is satisfied, processing advances to next Step 3.

10 Figs.7A to 7C are conceptual views of the all point replacement method.

 Explanation is made simply. Black dots in Figs.7A to 7C expresse the extreme value points used for the interpolation. The weighted approximation error $E(e^{j\omega})$ obtained from the extreme value points corresponds to the solid line.

 As illustrated in Fig.7A, values of the weighted approximation error at the extreme value points of the black dots become open circles. However, the actual extreme values are frequency indicated by black squares. Accordingly, the frequency indicated by the black squares is taken to be the new extreme value point, then returning to processing of Step 1.

 Further, as illustrated in Fig.7B, since there is a

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deviation of the frequency exists between the extreme value points used for the interpolation and the actual extreme value, the frequency indicated by the square is taken to be the new extreme value points, then returning
5 to processing of Step 1.

Then, as illustrated in Fig.7C, when the extreme value points used for the interpolation and the extreme value point (open circles) of the actual weighted approximation error become the same, and the repetition
10 processing terminals.

Step 3

Coefficients of the linear-phase FIR filter are found from the approximated amplitude characteristic (F 105).

When n-tap of impulse response $h(n)$ is found from
15 the optimum approximation function $P(e^{j\omega})$, the n-tap of impulse response is obtained from the following equation instead of $P(n)$.

$$H(e^{j\omega}) = P(e^{j\omega}) \cdot Q(e^{j\omega}) \cdot Z(e^{j\omega}) \quad (24)$$

20 Case 1:

$$h(n) = \frac{1}{N} \left\{ H(0) + 2 \sum_{k=1}^{\frac{N-1}{2}} (-1)^k H\left(\frac{2\pi}{N}k\right) \cos\left(\frac{2\pi}{N}k\left(n + \frac{1}{2}\right)\right) \right\} \quad (25)$$

Case 2:

$$h(n) = \frac{2}{N} \sum_{k=0}^{N-1} (-1)^k H\left(\frac{2\pi}{N}\left(k + \frac{1}{2}\right)\right) \sin\left(\frac{2\pi}{N}\left(k + \frac{1}{2}\right)\left(n + \frac{1}{2}\right)\right) \quad (26)$$

Case 3:

$$h(n) = -\frac{2}{N} \sum_{k=0}^{N-1} (-1)^k H\left(\frac{2\pi}{N}k\right) \sin\left(\frac{2\pi}{N}k\left(n + \frac{1}{2}\right)\right) \quad (27)$$

5

Case 4:

$$h(n) = \frac{2}{N} \sum_{k=0}^{N-1} (-1)^k H\left(\frac{2\pi}{N}\left(k + \frac{1}{2}\right)\right) \cos\left(\frac{2\pi}{N}\left(k + \frac{1}{2}\right)\left(n + \frac{1}{2}\right)\right) \quad (28)$$

Further, when the impulse response $k(n)$ of the
 10 equalizer of $L = N - (U - 1)$ tap is found, the following
 equation is calculated.

$$K(e^{j\omega}) = P(e^{j\omega}) \cdot Q(e^{j\omega}) \quad (29)$$

15

Case 1:

$$k(n) = \frac{1}{L} \left\{ K(0) + 2 \sum_{k=1}^{L-1} (-1)^k K\left(\frac{2\pi}{L}k\right) \cos\left(\frac{2\pi}{L}k\left(n + \frac{1}{2}\right)\right) \right\} \quad (30)$$

Case 2:

$$k(n) = \frac{2}{L} \sum_{k=0}^{\frac{L}{2}-1} (-1)^k K\left(\frac{2\pi}{L}\left(k + \frac{1}{2}\right)\right) \sin\left(\frac{2\pi}{L}\left(k + \frac{1}{2}\right)\left(n + \frac{1}{2}\right)\right) \quad (31)$$

Case 3:

$$k(n) = -\frac{2}{L} \sum_{k=0}^{\frac{L}{2}-1} (-1)^k K\left(\frac{2\pi}{L}k\right) \sin\left(\frac{2\pi}{L}k\left(n + \frac{1}{2}\right)\right) \quad (32)$$

5

Case 4:

$$k(n) = \frac{2}{L} \sum_{k=0}^{\frac{L}{2}-1} (-1)^k K\left(\frac{2\pi}{L}\left(k + \frac{1}{2}\right)\right) \cos\left(\frac{2\pi}{L}\left(k + \frac{1}{2}\right)\left(n + \frac{1}{2}\right)\right) \quad (33)$$

As to the pre-filter, when the transfer function Z
 10 (n) is 1 as indicated in the following equation, the
 Remez Exchange algorithms in question is substantially
 equal to a normal Remez Exchange algorithms.

$$Z(z) = 1 \quad (34)$$

15

Here, comparison between the conventional technique
 and the method of the present invention is carried out by
 taking zero point for avoiding the Chessboard distortion
 to be the pre-filter.

20 The frequency response of the pre-filter is expressed
 as follows:

$$\begin{aligned}
 Z(e^{j\omega}) &= (1 + e^{-j\omega} + e^{-2j\omega} + \dots + e^{-j\omega(U-1)}) \\
 &= \begin{cases} 1 + \sum_{m=0}^{(U-1)/2} 2\cos(m\omega), & U: \text{odd} \\ \sum_{m=0}^{U/2} 2\cos\left\{m + \frac{1}{2}\right\}\omega\}, & U: \text{even} \end{cases} \quad (35)
 \end{aligned}$$

The specification of the conventional technique and
 5 the present invention are indicated below.

Fig.8 is a view illustrating frequency response of
 low-pass filter which avoids the chessboard distortion
 designed depending on the present invention. Figs.9A and
 9B are views for comparing the frequency response of the
 10 low-pass filter designed depending on the conventional
 technique with the present invention respectively. Fig.10
 is a view illustrating weighted approximation error to
 the filter designed depending on the present invention.

Specification of the conventional technique

15 Linear-phase FIR filter of equalizer

- 22 taps
- even symmetry

Method of Design

The equalizer is made to design with the Remez
 20 Exchange algorithms, thus the pre-filter of zero point is
 folded into the linear-phase FIR filter in order to avoid
 the chessboard distortion of $U = 3$. Finally, the linear-

phase FIR filter with 24 taps is designed.

[Table 1]

Band

5

Band	Range of frequency	gain	weight
1	$0 \leq \omega \leq 0.3\pi$	1	1
2	$0.5\pi \leq \omega \leq \pi$	0	1

10

In Figs.9A and 9B, the conventional technique is illustrated by dotted line written as "Conventional".

Specification of the present invention

Linear-phase FIR filter

15

- 24 taps
- even symmetry
- $U = 3$

Method of Design

20

Designing has been attempted with Remez Exchange algorithms by taking into account the frequency response of the pre-filter of zero point for avoiding the chessboard distortion.

25

[Table 2]

Band

Band	Range of frequency	gain	weight
1	$0 \leq \omega \leq 0.3\pi$	1	1
2	$0.5\pi \leq \omega \leq \pi$	0	1

The dotted lines in Fig.8 and Figs. 9A and 9B
 indicate the frequency characteristic of the pre-filter
 and the frequency characteristics of the equalizer of the
 zero point for avoiding the chessboard distortion. The
 solid lines indicate both the frequency characteristic
 (Proposed $H(z)$) obtained finally and the frequency (Zero
 Point) that must be $H(z) = 0$ for avoiding the chessboard
 distortion.

As seen from Fig.8 to Fig.10, the method of the
 present invention is capable of obtaining good frequency
 response characteristic compared with the conventional
 technique.

Next, as a modified example, an algorithm which
 satisfies an attenuation quantity of the designated stop
 band will be explained.

This algorithm is an algorithm satisfies the
 attenuation quantity (weighted approximation error) of
 the designated stop band in connection with the low-pass

filter with 2 numbers of bands or the high-pass filter by using the Remez Exchange algorithms which takes into account the frequency response of the pre-filter.

Further, in later explanation, description is made
 5 for the low-pass filter, however, when the algorithms is intended to apply to the high-pass filter, the pass-band and the block-band are inversely related.

As a method for satisfying an attenuation quantity of the stop band, there exists three kinds of approaches.

10 The first approach is that the end frequency ω_p of the pass band is made variable, the starting frequency ω_s of the stop band is made to be fixed, and the number of taps is made to be fixed.

The second approach is that the end frequency ω_p of
 15 the pass band is made to be fixed, the starting frequency ω_s of the stop band is made variable, and the number of taps is made to be fixed.

The third approach is that the end frequency ω_p of the pass band is made to be fixed, the starting frequency
 20 ω_s of the stop band is made to be fixed, and the number of taps is made variable.

The first, the second, and the third approaches are explained below with reference to the accompanying drawings successively.

25 First Approach

In the first approach, the maximum end frequency ω_p of the pass band that satisfies the attenuation quantity dBs of the designated stop band is found.

Fig.11 is a view illustrating flowchart of algorithms
 5 for finding filter that satisfies the attenuation quantity of the stop band.

Fig.12 is a view illustrating flowchart of algorithms for finding filter that has the maximum end frequency of the pass band, which end frequency satisfies the
 10 attenuation quantity of the stop band, in which free parameters (variable) and fixed parameter (variable) are expressed.

Here, free parameters in the algorithms, object, and the principle of the algorithms are enumerated as
 15 follows:

- * Free parameters: end frequency ω_p of the pass band.
- * Object: it is an object to obtain a filter that has the maximum end frequency ω_p of the pass band, which end frequency satisfies the attenuation quantity of the
 20 designated stop band.

- * Principle: the starting frequency of the pass band and the frequencies of both ends of the stop band are fixed, and the end frequency of the pass band is the free parameter. In the Chebyshev approximation according to
 25 the Remez Exchange algorithms,

- the end frequency ω_p of the pass band moves far away rather than the starting frequency ω_s

→ the attenuation quantity of the stop band becomes large.

5 • the end frequency ω_p of the pass band approaches the starting frequency ω_s of the stop band

→ the attenuation quantity of the stop band becomes small.

Namely, $\omega_p^{(cur)}$ is made to prepare at the frequency (in
 10 the vicinity of $\omega = 0$) which is far from the starting frequency ω_s of the stop band. While, $\omega_p^{(pre)}$ which is close to the starting frequency of the stop band is made to prepare as initial frequency. Then, the position ω_p of the maximum end frequency is found within the pass band
 15 that satisfies the designated attenuation quantity while utilizing the dichotomizing method.

Further, the golden section method is the most efficient method in the line search methods of such parameter. However, the dichotomizing (two branching)
 20 method is adopted here. The dichotomizing method has the algorithms which is easy to understand.

Fig.11 and contents of each step processing F 102, F 103, F 104, F 105 of the algorithms described hereinafter are the same as the Remez Exchange algorithms under
 25 taking into account the frequency response of the pre-

filter described in relation to Fig.6. Accordingly, the same signs as that of Fig.6 are used in connection with these processing.

Step 10

5 As illustrated in Fig.11, firstly, initial setting is executed (F 201). In this initial setting, setting of the linear-phase FIR filter, setting of the band, setting of the coefficient of the pre-filter, setting of the initial extreme value point, designation of the attenuation
10 quantity of the stop band, and setting of the initial frequency of the dichotomizing method are executed.

Concrete items thus set are as follows:

- the number of tap
- linear-phase FIR filter with even symmetry or odd
15 symmetry
 - the number of the band is two
 - the starting frequency of the pass band
 - gain of the pass band
 - frequencies of both ends of the stop band
 - 20 • gain of the stop band
 - weighting in connection with the pass band and the stop band
 - coefficients of the pre-filter
 - attenuation quantity dBs (namely, pointing
25 largeness δ_2 of ripple of the stop band)

• frequency $\omega^{(0)} = \omega_k^{(0)}$ ($k = 0, \dots, R$) that becomes the extreme value in the approximation band. Provided letter of right shoulder (i) expresses the number of repetition.

5 Also, Fig.13 is a view illustrating initial frequency of the dichotomizing method in the algorithms for finding filter having the maximum end frequency of the pass band that satisfies the attenuation quantity of the stop band.

As illustrated in Fig.13, in the present example, the
10 following values are given as the initial frequencies of the dichotomizing method.

$\omega_p^{(pre)}[0]$ = the vicinity of starting frequency of the
stop band (37)

15 $\omega_p^{(cu)}[0]$ = the vicinity of starting frequency of the
pass band (38)

Portion of [t] at the back of ω_p expresses the number of cycle.

20 Here, the Remez Exchange algorithms taking into account the frequency response of the pre-filter is executed to the frequency $\omega_p^{(pre)}[0]$, thus the minimum of the attenuation quantity $dB^{(pre)}[0]$ in the stop band is found. The following steps are explained on the basis of

the assumption.

Step 11

The Remez Exchange algorithms taking into account the frequency response of the pre-filter is executed (F 102, 5 F 103, F 104).

Concretely, in the processing F 102, the interpolation polynomial expression is generated for interpolating an the amplitude characteristic from the extreme value point at the time of $\omega_p^{cur}[t]$.

10 Subsequently, in the processing F 103, the new extreme value point is determined from the amplitude characteristic obtained from the interpolation polynomial expression.

Then, in the processing F 104, the repetition 15 judgement of the Remez Exchange algorithms is executed.

Step 12

Next, the attenuation quantity of the stop band is examined (F 206).

The minimum attenuation quantity (the maximum 20 weighted approximation error δ_2) $dB_s^{(cur)}[t]$ is examined in the stop band by using the interpolation polynomial expression founded in the processing F 102.

Step 13

Next, comparison is attempted in connection with the 25 attenuation quantity of the designated stop band (F 207).

Concretely, in the case that the result of the comparison satisfies the following equations (39) or (40) while comparing with the attenuation quantity dBs of the designated stop band, processing is moved to processing of Step 15 (F 105). While when the result of the comparison does not satisfy equations (39) or (40), processing is moved to processing of Step 14 (F 208).

$$\left| dB_s^{(cur)}[t] - dB_s \right| < \varepsilon_1 \quad (39)$$

$$\left| \omega_p^{(cur)}[t] - \omega_p^{(pre)}[t] \right| < \varepsilon_2 \quad (40)$$

Provided that ε_1 and ε_2 are extremely small values.

Step 14

Setting of the band is changed when the result of the comparison does not satisfy equations (39) or (40), in the comparison to the attenuation quantity dBs of the designated stop band (F 208).

Concretely, the end frequency $\omega_p^{cur}[t+1]$ of new pass band is made to set. Explanation is made while dividing into two cases of the first loop and the second loop as the setting method.

First time:

In the case of the first time, there are three cases illustrated in Figs.14A to 14C.

Namely, cases illustrated in Fig.14A, Fig.14B, and Fig.14C are considered in connection with the frequencies $\omega_p^{(pre)}[0]$, $\omega_p^{(cur)}[0]$.

The case illustrated in Fig.14A is one in which the
5 both satisfy the designated attenuation quantity. In this case, the frequency $\omega_p^{(pre)}[0]$ close to the starting frequency ω_s of the stop band is taken to be solution, thus advancing toward to the processing of Step 15.

The case illustrated in Fig.14B is one in which the
10 both do not satisfy the designated attenuation quantity. In this case, the present number of taps can not realize the designated attenuation quantity. Accordingly, that effect is indicated to end processing.

The case illustrated in Fig.14C is one in which only
15 one side satisfies the designated attenuation quantity. In this case, processing is moved to Step 11 in such a way as following equation (41).

Further, in the present method for giving initial frequency point, there is no case in which $\omega_p^{(pre)}[0]$ is
20 satisfied and $\omega_p^{(cur)}[0]$ is not satisfied.

$$\begin{aligned}\omega_p^{(pre)}[1] &= \omega_p^{(cur)}[0] \\ \omega_p^{(cur)}[1] &= 0.5 \times (\omega_p^{(cur)}[0] + \omega_p^{(pre)}[0]) \\ dB^{(pre)}[1] &= dB^{(cur)}[0]\end{aligned}\tag{41}$$

Second time and later:

In the case of second time and later, two cases indicated in Figs.15A and 15B are considered. In the determining method of the new frequency in the second
 5 time and later, the frequency which satisfies the designated attenuation quantity dBs is preserved invariably within $\omega_p^{(pre)}[t+1]$. The case illustrated in Fig.15A, Fig.15B is considered in connection with the frequencies $\omega_p^{(pre)}[t]$, $\omega_p^{(cur)}[t]$.

10 The case illustrated in Fig.15A is one in which one side satisfies the designated attenuation quantity. In this case, the processing is moved to next step 11 in such a way as the following equation (42).

Further, since the frequency which satisfies the
 15 designated attenuation quantity always conforms to $\omega_p^{(pre)}[t]$, there does $\omega_p^{(pre)}[t]$ not exist the case that does not satisfy.

$$\begin{aligned}\omega_p^{(pre)}[t+1] &= \omega_p^{(pre)}[t] \\ \omega_p^{(cur)}[t+1] &= 0.5 \times (\omega_p^{(cur)}[t] + \omega_p^{(pre)}[t]) \\ dB^{(pre)}[t+1] &= dB^{pre}[t]\end{aligned}\quad (42)$$

20 The case illustrate in Fig.15B is one in which the both satisfies the designated attenuation quantity. In this case, the processing is moved to next step 11 in

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such a way as the following equation (43).

$$\begin{aligned}\omega_p^{(pre)}[t+1] &= \omega_p^{(cur)}[t] \\ \omega_p^{(cur)}[t+1] &= \omega_p^{(cur)}[t] + 0.5 \times (\omega_p^{(cur)}[t] - \omega_p^{(pre)}[t]) \\ dB^{(pre)}[t+1] &= dB^{(cur)}[t]\end{aligned}\tag{43}$$

5 Step 15

The coefficients of the linear-phase FIR filter is obtained from the approximated amplitude characteristic (F 105).

Namely, the coefficients of the linear-phase FIR
10 filter is obtained from the amplitude characteristic obtained finally.

Fig.16 is a view illustrating frequency response characteristic of the low-pass filter obtained from the algorithms for obtaining "filter having the maximum end
15 frequency of the pass band that satisfies the attenuation quantity of the stop band" while taking the filter of the zero point for avoiding the chessboard distortion.

Fundamental algorithms, variable intended to find, and band of this case are as follows:

20 Fundamental algorithms

It is the Remez Exchange algorithms taking into account frequency characteristic of the pre-filter.

- 24 taps

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- even symmetry
- $U = 3$ (filter coefficient is executed U times such that DC gain becomes U)
- attenuation quantity of the stop band is not more than - 40 dB

Variable intended to find

It is the end frequency ω_p of the pass band.

[Table 3]

<u>Band</u>			
band	Frequency region	gain	weight
Pass band	$0 \leq \omega \leq \omega_p$	1	1
Stop band	$0.5\pi \leq \omega \leq \pi$	0	1

Further, in Fig.16, the solid line indicates frequency response of low-pass filter that has the maximum end frequency of the pass band which satisfies the attenuation quantity of the stop band. Furthermore, the dotted line indicated by ① indicates frequency which becomes zero point for avoiding the chessboard distortion, and the dotted line indicated by ② indicates period of the band given beforehand.

As seen from Fig.16, the low-pass filter which is obtained from the algorithms for finding "filter having the maximum end frequency of the pass band which satisfies the attenuation quantity of the stop band"

according to the present invention has a good frequency response characteristic.

Second approach

Next, in the second approach, the minimum starting
5 frequency ω_s of the stop band that satisfies the attenuation quantity dBs of the designated stop band is found.

The flowchart for this attempt is equivalent to that of Fig.11 referred to in the first approach.

10 Fig.17 shows a free parameter (variable) and fixed parameter (variable) in the algorithms for finding filter having the minimum starting frequency of the stop band that satisfies the attenuation quantity of the stop band.

Here, the free parameter of this algorithms, objects,
15 and the principle of the algorithms thus enumerated are as follows:

* free parameter: it is the starting frequency ω_s of the stop band.

* objects: it is an object to obtain filter having
20 the minimum starting frequency ω_s of the stop band that satisfies attenuation quantity of the designated stop band.

* principle: the end frequency of the stop band and the frequencies of both ends of the pass band are fixed,
25 and the starting frequency of the stop band is the free

parameter. In the Chebyshev approximation according to the Remez Exchange algorithms,

- the starting frequency ω_s of the stop band moves far away rather than the end frequency ω_p of the pass band \rightarrow the attenuation quantity of the stop band becomes large.

- the starting frequency ω_s of the stop band approaches the end frequency ω_p of the pass band \rightarrow the attenuation quantity of the stop band becomes small.

10 Namely, $\omega_s^{(pre)}$ is made to prepare that is far from the end frequency of the pass band. While, $\omega_s^{(cur)}$ which is close to the end frequency of the pass band is made to prepare as initial frequencies. Then, position ω_s of the minimum starting frequency is found within the stop band
15 that satisfies the designated attenuation quantity while utilizing the dichotomizing method.

Further, the golden section method is the most efficient method in the line search methods of such parameter. However, the dichotomizing method is made to
20 adopt here. The dichotomizing method has the algorithms which is easy to understand.

Also, Fig.11 and contents of each step processing F 102, F 103, F 104, F 105 of the algorithms described hereinafter are the same as the Remez Exchange algorithms
25 while taking into account the frequency response of the

pre-filter described in relation to Fig.6 in the same way as the case of the first approach. Accordingly, the same signs as that of Fig.6 are used in connection with these processing.

5 Step 20

As illustrated in Fig.11, firstly, initial setting is executed (F 201). In this initial setting, setting of the linear-phase FIR filter, setting of the band, setting of a coefficient of the pre-filter, setting of the initial
10 extreme value point, designation of attenuation quantity of the stop band, and setting of initial frequency of dichotomizing method are executed.

Concrete items thus set are as follows:

- the number of taps
- 15 • linear-phase FIR filter with even symmetry or odd symmetry
- the number of the bands is two
- the starting frequency of the pass band
- gain of the pass band
- 20 • frequencies of both ends of the stop band
- gain of the stop band
- weighting to the pass band and the stop band
- coefficients of the pre-filter
- attenuation quantity dBs (namely, pointing
- 25 largeness δ_2 of ripple of the stop band)

• frequency $\omega^{(0)} = \omega_k^{(0)}$ ($k = 0, \dots, R$) that becomes the extreme value in the approximation band. Provided letter of right shoulder (i) expresses the number of repetition.

5 Also, Fig.18 is a view illustrating initial frequency of the dichotomizing method in the algorithms for finding filter having the minimum starting frequency of the stop band that satisfies the attenuation quantity of the stop band.

10 As illustrated in Fig.18, in the present example, the following values are given as the initial frequencies of the dichotomizing method.

$\omega_s^{(p)}[0]$ = the vicinity of end frequency of the pass
band (44)

$\omega_s^{(cur)}[0]$ = the vicinity of end frequency of the
stop band (45)

Portion of [t] at the back of ω_s expresses the number
20 of cycle.

Here, the Remez Exchange algorithms taking into account the frequency response of the pre-filter is executed to the frequency $\omega_s^{(pre)}[0]$, thus the minimum of the attenuation quantity $dB^{(pre)}[0]$ in the stop band is

found. The following steps are explained on the basis of this assumption.

Step 21

The Remez Exchange algorithms taking into account the
5 frequency response of the pre-filter is executed (F 102, F 103, F 104).

Concretely, in the processing F 102, the
interpolation polynomial expression is generated for
interpolating an amplitude characteristic from the
10 extreme value point at the time of $\omega_s^{(cur)}[0]$.

Subsequently, in the processing F 103, the new
extreme value point is determined from the amplitude
characteristic obtained from the interpolation polynomial
expression.

15 Then, in the processing F 104, repetition judgement
of the Remez Exchange algorithms is executed.

Step 22

Next, the attenuation quantity of the stop band is
examined (F 206).

20 The minimum attenuation quantity (the maximum
weighted approximation error δ_2) $dB_s^{(cur)}[t]$ is examined in
the stop band while using the interpolation polynomial
expression founded in the processing F 102.

Step 23

Next, comparison to the attenuation quantity of the designated stop band is executed (F 207).

Concretely, in the case that result of the comparison satisfies following equations (46) or (47) while
 5 comparing with the attenuation quantity dBs of the designated stop band, processing is moved to processing of Step 25 (F 105). While when result of the comparison does not satisfy equations (46) or (47), processing is moved to processing of Step 24 (F 208).

10

$$|dB_s^{(cur)}[t] - dB_s| < \varepsilon_1 \quad (46)$$

$$|\omega_s^{(cur)}[t] - \omega_s^{(pre)}[t]| < \varepsilon_2 \quad (47)$$

15 Provided that ε_1 and ε_2 are extremely small values.

Step 24

Setting of the band is changed when the result of the comparison does not satisfy equations (46) or (47), in the comparison to the attenuation quantity dBs of the
 20 designated stop band (F 208).

Concretely, the starting frequency $\omega_s^{(cur)}[t+1]$ of new stop band is made to set. Explanation is made while dividing into two cases of the first loop and the second loop as the setting method.

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First time:

In the case of the first time, there are three cases illustrated in Figs.19A to 19C.

Namely, cases illustrated in Fig.19A, Fig.19B, and
 5 Fig.19C are considered to frequencies $\omega_s^{(prd)}[0]$, $\omega_s^{(cu)}[0]$.

The case illustrated in Fig.19A is one in which the both satisfy the designated attenuation quantity. In this case, the frequency $\omega_s^{(pre)}[0]$ close to $\omega=0$ is taken to be solution, thus advancing toward to the processing of Step

The case illustrated in Fig.19B is one in which the both do not satisfy the designated attenuation quantity. In this case, the present number of taps can not realize the designated attenuation quantity. Accordingly, that effect is indicated to end.

The case illustrated in Fig.19C is one in which only one side satisfies the designated attenuation quantity. In this case, processing is moved to Step 21 in such a way as following equation (48).

20 Further, in the present method for giving initial frequency point, the case in which $\omega_s^{(pre)}[0]$ is satisfied and $\omega_s^{(cur)}[0]$ is not satisfied does not exist.

$$\begin{aligned}
\omega_s^{(pre)}[1] &= \omega_s^{(cur)}[0] \\
\omega_s^{(cur)}[1] &= 0.5 \times (\omega_s^{(cur)}[0] + \omega_s^{(pre)}[0]) \\
dB_s^{(pre)}[1] &= dB_s^{(cur)}[0]
\end{aligned} \tag{48}$$

Second time and later:

In the case of second time and later, two cases
5 indicated in Figs.20A and 20B are considered. In the
determining method of the new frequency in the second
time and later, the frequency which satisfies the
attenuation quantity dBs thus designated is preserved
invariably within $\omega_s^{(pre)}[t+1]$. The case illustrated in
10 Fig.20A, Fig.20B is considered to the frequencies
 $\omega_s^{(pre)}[t], \omega_s^{(cur)}[t]$.

The case illustrated in Fig.20A is one in which one
side satisfies the designated attenuation quantity. In
this case, the processing is moved to next step 21 in
15 such a way as the following equation (49).

Further, since the frequency which satisfies the
designated attenuation quantity always conforms to
 $\omega_s^{(pre)}[t]$, the case that $\omega_s^{(pre)}[t]$ does not satisfy does not
exist.

$$\begin{aligned}
\omega_s^{(pre)}[t+1] &= \omega_s^{(pre)}[t] \\
\omega_s^{(cur)}[t+1] &= 0.5 \times (\omega_s^{(cur)}[t] + \omega_s^{(pre)}[t]) \\
dB_s^{(pre)}[t+1] &= dB_s^{(cur)}[t]
\end{aligned} \tag{49}$$

The case illustrate in Fig.20B is one in which the both satisfies the designated attenuation quantity. In this case, the processing is moved to next step 21 in such a way as the following equation (50).

5

$$\begin{aligned}\omega_s^{(pre)}[t+1] &= \omega_s^{(cur)}[t] \\ \omega_s^{(cur)}[t+1] &= \omega_s^{(cur)}[t] + 0.5 \times (\omega_s^{(cur)}[t] - \omega_s^{(pre)}[t]) \\ dB_s^{(pre)}[t+1] &= dB_s^{(cur)}[t]\end{aligned}\quad (50)$$

Step 25

The coefficients of the linear-phase FIR filter are found from the approximated amplitude characteristic (F 105).

Namely, the coefficients of the linear-phase FIR filter are found from the amplitude characteristic obtained finally.

Fig.21 is a view illustrating frequency response characteristic of the low-pass filter obtained from the algorithms for finding "filter having the minimum starting frequency of stop band which filter satisfies the attenuation quantity of the stop band" while taking the filter of the zero point for avoiding the chessboard distortion.

Fundamental algorithms, variables intended to find, and band of this case are as follows:

Fundamental algorithms

It is the Remez Exchange algorithms taking into account frequency characteristic of the pre-filter.

- 24 taps
- even symmetry
- $U = 3$ (filter coefficient is executed U times such that DC gain becomes U)
- attenuation quantity of the stop band is not more than - 40 dB

10 Variable intended to find

It is the starting frequency ω_s of the stop band.

[Table 4]

15

<u>Band</u>			
band	Frequency region	gain	weight
Pass band	$0 \leq \omega \leq 0.3\pi$	1	1
Stop band	$\omega_s \leq \omega \leq \pi$	0	1

Further, in Fig.21, the solid line indicates frequency response of low-pass filter that has the minimum starting frequency of the stop band which satisfies the attenuation quantity of the stop band. Furthermore, the dotted line indicated by ① indicates frequency which becomes zero point for avoiding the chessboard distortion, and the dotted line indicated by

25

② indicates period of the band given beforehand.

As seen from Fig.21, the low-pass filter which is obtained from the algorithms for finding "filter having the minimum starting frequency of the stop band which satisfies attenuation quantity of the stop band" according to the present invention has a good frequency response characteristic.

Third approach

Finally, in the third approach, the minimum number N of taps that satisfies the attenuation quantity dBs of the designated stop band is found.

Fig.22 is a view illustrating flowchart of the algorithms for finding filter with the minimum number of tap that satisfies the attenuation quantity of the stop band.

Here, free parameters of this algorithms, objects, and the principle of the algorithms thus enumerated are as follows:

- * free parameters: it is the number of taps
- * objects: it is an object to obtain filter having the minimum number of tap that satisfies attenuation quantity of the designated stop band.
- * principle: since variable of the band is fixed, when it is impossible to satisfy the attenuation quantity of the designated stop band, the number of tap is

increased by one tap.

Also, Fig.22 and contents of each step processing F 102, F 103, F 104, F 105 of the algorithms described hereinafter are the same as the Remez Exchange algorithms while taking into account the frequency response of the pre-filter described in relation to Fig.6 in the same way as the case of the first approach. Further, contents of processing F 206 is the same as the processing explained in relation to Fig.11 in the same way as the case of the second approach. Accordingly, the same signs as that of Fig.6 and Fig.11 are used in connection with these processing.

Step 30

As illustrated in Fig.22, firstly, initial setting is executed (F 401). In this initial setting, setting of linear-phase FIR filter, setting of band, setting of coefficient of the pre-filter, setting of the initial extreme value point, and designation of attenuation quantity of the stop band, are executed.

Concrete items thus set are as follows:

- the number of initial tap
- linear-phase FIR filter with even symmetry or odd symmetry
- the number of the band is two
- the starting frequency and end frequency of

respective bands

- gain of respective bands
- weighting of respective bands
- coefficient of the pre-filter
- 5 • attenuation quantity dBs (namely, pointing largeness δ_2 of ripple of the stop band)
- frequency $\omega^{(0)} = \omega_k^{(0)}$ ($k = 0, \dots, R$) that becomes the extreme value in the approximation band. Provided letter of right shoulder (i) expresses the number of
- 10 repetition.

Step 31

The Remez Exchange algorithms taking into account the frequency response of the pre-filter is executed (F 102, F 103, F 104).

- 15 Concretely, in the processing F 102, the interpolation polynomial expression is generated for interpolating an amplitude characteristic from the extreme value point at the time of $\omega_p^{(cur)}[t]$.

- 20 Subsequently, in the processing F 103, the new extreme value point is determined from the amplitude characteristic obtained from the interpolation polynomial expression.

Then, in the processing F 104, repetition judgement of the Remez Exchange algorithms is executed.

- 25 Step 32

Next, the attenuation quantity of the stop band is examined (F 206).

The minimum attenuation quantity (the maximum weighted approximation error δ) $dB_s^{(cur)}[t]$ is examined in the stop band while using the interpolation polynomial expression founded in the processing F 102.

Step 33

Next, comparison to the attenuation quantity of the designated stop band is executed (F 412).

10 Concretely, in the case that result of the comparison
satisfies the following equations (51) while comparing
with the attenuation quantity dBs of the designated stop
band, processing is moved to processing of Step 35 (F
105). While when result of the comparison does not
15 satisfy equations (51), processing is moved to processing
of Step 34 (F 413).

$$|dB_s^{(cur)}[t]\rangle \langle dB_s| \quad (51)$$

Step 34

20 One tap is increased (F 413).

Namely, one tap is increased in addition to the present number of tap, thus processing is moved to processing of Step 31.

Step 35

25 The coefficients of the linear-phase FIR filter is

found from the approximated amplitude characteristic (F
105).

Namely, the coefficients of the linear-phase FIR
filter is found from the amplitude characteristic
5 obtained finally.

Fig.23 is a view illustrating frequency response
characteristic of the low-pass filter obtained from the
algorithms for finding "the minimum number of tap that
satisfies attenuation quantity of the stop band" while
10 taking the filter of the zero point for avoiding the
chessboard distortion.

Fundamental algorithms, variables intended to find,
and band of this case are as follows:

Fundamental algorithms

15 It is the Remez Exchange algorithms taking into
account frequency characteristic of the pre-filter.

- the number of initial tap is 10 taps
- even symmetry
- $U = 3$ (filter coefficient is executed U times

20 such that DC gain becomes U)

- attenuation quantity of the stop band is not more
than - 60 dB

Variables intended to find

It is the number N of tap.

[Table 5]

Band

band	Frequency region	gain	weight
Pass band	$0 \leq \omega \leq 0.3\pi$	1	1
Stop band	$0.5\pi \leq \omega \leq \pi$	0	1

5

Further, in Fig.23, the solid line indicates frequency response of low-pass filter of the minimum number of tap (36 taps) in which the attenuation quantity of the stop band becomes not more than -60 dB.

10

Furthermore, the dotted line indicated by ① indicates frequency which becomes zero point for avoiding the chessboard distortion, and the dotted line indicated by ② indicates period of the band given beforehand.

15

As known from Fig.23, the low-pass filter which is obtained from the algorithms for finding "the minimum number of tap which realizes attenuation quantity of the stop band" according to the present invention has good frequency response characteristic.

20

Subsequently, as the second modified example, explanation is performed about algorithms for finding filter that causes the signal to pass frequency point of transition band that satisfies attenuation quantity of the stop band.

25

Here, followings are free parameter in the

* Free parameter: end frequency ω_p of the pass band
and starting frequency ω_s of the stop band.

* Principle: the starting frequency of the pass band and the end frequency of the stop band are fixed, and the end frequency ω_p of the pass band and the starting
15 frequency ω_s of the stop band are the free parameters. Since there are two free parameters, it is impossible to determine appropriately if moving simultaneously.

Accordingly, one side of parameter is fixed, while the other side of parameter that satisfies attenuation quantity of the stop band is found. When the band does not make the attenuation quantity dBc with the frequency ω_c of the transition band pass through, it causes the fixed parameter to be changed. Above repetition is carried out so that the band which makes the attenuation quantity dBc with the frequency ω_c of the transition band

pass through is determined.

In the method for finding parameter that satisfies the attenuation quantity of the stop band, there are two kinds of approaches.

5 Namely, the first approach is that filter which has the minimum starting frequency of the stop band that satisfies the attenuation quantity of the stop band is found.

10 The second approach is that filter which has the maximum end frequency of the pass band that satisfies the attenuation quantity of the stop band is found.

Algorithms on the basis of the above two kinds of approaches are explained successively.

15 Fig.24 is a flowchart of algorithms for finding filter

That satisfies the attenuation quantity of the stop band and that enables the signal to be passed through the frequency point of the transition band.

20 The algorithms on the basis of the filter having the minimum starting frequency of the stop band that satisfies the attenuation quantity of the stop band will be explained in relation to Fig.24 to Fig.29.

Namely, the present algorithms utilizes the algorithms for finding "filter having the minimum
25 starting frequency of the stop band that satisfies the

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attenuation quantity of the stop band".

The concrete course of the algorithms, as illustrated in Fig.25, ω_s is obtained with aforementioned algorithms as inner loop, further loop for finding ω_p is put on
 5 outside thereof to determine parameter of the band. Namely, the outside loop causes the end frequency ω_p of the pass band to be fixed, while the inner loop causes the starting frequency ω_s of the stop band to be found that satisfies the attenuation quantity dBs of the stop
 10 band.

When the amplitude characteristic thus found does not pass through the designated point (ω_c , dBc) of the transition band, ω_p is searched while using dichotomizing method like the case of searching "filter having the
 15 maximum end frequency of the pass band that satisfies the attenuation quantity of the stop band".

Hereinafter, concrete algorithms is indicated, however, since the algorithms for finding "filter having the minimum starting frequency of the stop band that
 20 satisfies the attenuation quantity of the stop band" to be the inner loop is the same as that described above, thus description thereof is omitted.

Also, the content of Fig.24 and each step processing F 102, F 103, F 104, and F 105 of the algorithms
 25 explained below, like the case of the first approach, is

the same as the Remez Exchange algorithms taking into account the frequency response of the pre-filter explained in relation to Fig.6. Further, the content of each processing F 206, F 207, F 208, like the case of the second approach, is the same as processing explained in relation to Fig.11 namely the algorithms of "filter having the minimum starting frequency of the stop band that satisfies the attenuation quantity of the stop band". Accordingly, as for this processing, the same marks as Fig.6 and Fig.11 are used.

Step 40

As illustrated in Fig.24, firstly, initial setting is executed (F 301). In this initial setting, setting of linear-phase FIR filter, setting of band, setting of coefficient of the pre-filter, setting of the initial extreme value point, designation of attenuation quantity of the stop band, and setting of initial frequency of dichotomizing method are executed.

Concrete items thus set are as follows:

- the number of tap
- linear-phase FIR filter with even symmetry or odd symmetry
- the number of the band is two
- the starting frequency of the pass band $\omega = 0$
- gain of the pass band

- the end frequency of the stop band $\omega = \pi$
 - gain of the stop band
 - weighting to the pass band and the stop band
 - coefficient of the pre-filter
- 5 • attenuation quantity dBs of the stop band (namely, pointing largeness δ_2 of ripple of the stop band)
- frequency ω_c of the transition band and attenuation quantity dBc thereof
 - frequency $\omega^{(0)} = \omega_k^{(0)}$ ($k = 0, \dots, R$) that becomes
- 10 the extreme value in the approximation band. Provided letter of right shoulder (i) expresses the number of repetition.

Also, Fig.26 is a view illustrating initial frequency of the dichotomizing method in the algorithms for finding

15 filter that causes the signal to pass the frequency point of the transition band, and that satisfies the attenuation quantity of the stop band.

As illustrated in Fig.26, in the present example, following values are given as the initial frequencies of

20 the dichotomizing method.

$$\omega_p^{(prc)}[0] = \text{the vicinity of starting frequency of the pass band} \quad (52)$$

$$\omega_p^{(cut)}[0] = \text{the vicinity of } \omega_c \quad (53)$$

Portion of $[t]$ at the back of ω_p expresses the number of cycle.

Here, the Remez Exchange algorithms taking into account the frequency response of the pre-filter is
 5 executed to the frequency $\omega_p^{(pre)}[0]$, thus the minimum starting frequency $\omega_s^{(pre)}[0]$ of the stop band that satisfies the designated attenuation quantity dBs in the stop band is found, the gain $dB_c^{(cur)}[0]$ corresponding to ω_c at this time is found. The following steps are explained
 10 on the basis of this assumption.

Step 41

The algorithms for finding "filter having the minimum starting frequency of the stop band that satisfies the attenuation quantity of the stop band" is executed (F
 15 102, F 103, F 104, F206, F 207, F 208).

Concretely, in the processing F 102, interpolation polynomial expression is generated for interpolating an amplitude characteristic from the extreme value point at the time of $\omega_p^{(cur)}[t]$.

20 Subsequently, in the processing F 103, the new extreme value point is determined from the amplitude characteristic obtained from the interpolation polynomial expression.

Then, in the processing F 104, repetition judgement

of the Remez Exchange algorithms is executed.

Next, in the processing F 206, the minimum attenuation quantity is found in the stop band.

Next, in the processing F 207, end condition of the
5 algorithms for finding filter having the minimum starting frequency ω_s of the stop band that satisfies the attenuation quantity of the stop band is obtained.

Also, in the processing F 208, setting of the starting frequency $\omega_s^{(cur)}$ of the new stop band is
10 executed.

Step 42

Next, the attenuation quantity of the frequency that is designated as the transition band (F 309) is examined.

In the processing F 102, the attenuation quantity
15 $dB_c^{(cur)}[t]$ to the frequency ω_c which is designated as the transition band while using LaGrange's interpolation polynomial expression found finally with the algorithms for finding "the minimum starting frequency of the stop band that satisfies the attenuation quantity of the stop
20 band" is examined.

Step 43

Comparison to the designated attenuation quantity of the transition band is executed (F 310).

Concretely, in the case that result of the comparison
25 satisfies following equations (54) or (55) processing is

moved to processing of Step 45 (F 105). While when result of the comparison does not satisfy equations (54) or (55), processing is moved to processing of Step 44 (F 311).

5

$$|dB_c^{(cur)}[t] - dB_c| < \varepsilon_1 \quad (54)$$

$$|\omega_p^{(cur)}[t] - \omega_p^{(pre)}[t]| < \varepsilon_2 \quad (55)$$

10 Provided that ε_1 and ε_2 are extremely small values.

Step 44

Setting of the band is changed when result of the comparison does not satisfy equations (54) or (55), in the comparison between the frequency ω_c of the transition
 15 band and the attenuation quantity dBc (F 311).

Concretely, the end frequency $\omega_p^{(cur)}[t+1]$ of new pass band is made to set. Explanation is performed while dividing into two cases of the first loop and the second loop as the setting method.

20 First time:

In the case of the first time, there are three cases illustrated in Figs.27A to 27C.

Namely, cases illustrated in Fig.27A, Fig.27B, and Fig.27C are considered to frequencies

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$$\omega_p^{(pre)}[0], \omega_p^{(cur)}[0].$$

The case illustrated in Fig.27A is one in which the both satisfy the designated attenuation quantity dBc. In this case, the large frequency $\omega_p^{(cur)}[0]$ is taken to be
 5 solution, thus advancing toward the processing of Step 45.

The case illustrated in Fig.27B is one in which the both do not satisfy the designated attenuation quantity. In this case, the present number of taps can not realize
 10 the designated attenuation quantity. Accordingly, that effect is indicated to end.

The case illustrated in Fig.27C is one in which only one side satisfies the designated attenuation quantity. In this case, processing is moved to Step 41 in such a
 15 way as following equation (56).

Further, in the present method for giving initial frequency point, there does not exist the case in which $\omega_p^{(cur)}[0]$ is satisfied and $\omega_p^{(pre)}[0]$ is not satisfied.

$$\begin{aligned} \omega_p^{(pre)}[1] &= \omega_p^{(cur)}[0] \\ \omega_p^{(cur)}[1] &= 0.5 \times (\omega_p^{(cur)}[0] + \omega_p^{(pre)}[0]) \\ dB_c^{(pre)}[1] &= dB_c^{(pre)}[0] \end{aligned} \quad (56)$$

20

Second time and later:

In the case of second time and later, two cases indicated in Figs.28A and 28B are considered. In the determining method of the new frequency $\omega_p^{(cur)}[t+1]$ in the second time and later, the frequency which satisfies the
 5 attenuation quantity dBc thus designated is preserved invariably within $\omega_p^{(pre)}[t+1]$. The case illustrated in Fig.28A, the characteristic shown in Fig.28B is considered to the frequencies $\omega_p^{(pre)}[t]$ $\omega_p^{(cur)}[t]$.

The case illustrated in Fig.28A is one in which one
 10 side satisfies the designated attenuation quantity. In this case, the processing is moved to next step 41 in such a way as the following equation (57).

Further, since the frequency which satisfies the designated attenuation quantity always conforms to
 15 $\omega_p^{(pre)}[t]$, the case that $\omega_p^{(pre)}[t]$ does not satisfy does not exist.

$$\begin{aligned}\omega_p^{(pre)}[t+1] &= \omega_p^{(pre)}[t] \\ \omega_p^{(cur)}[t+1] &= 0.5 \times (\omega_p^{(cur)}[t] + \omega_p^{(pre)}[t]) \\ dB_c^{(pre)}[t+1] &= dB_c^{(pre)}[t]\end{aligned}\quad (57)$$

The case illustrated in Fig.28B is one in which the
 20 both satisfies the designated attenuation quantity. In this case, the processing is moved to next step 41 in such a way as the following equation (58).

$$\begin{aligned}
\omega_p^{(pre)}[t+1] &= \omega_p^{(cur)}[t] \\
\omega_p^{(cur)}[t+1] &= \omega_p^{(cur)}[t] + 0.5 \times (\omega_p^{(cur)}[t] - \omega_p^{(pre)}[t]) \\
dB_c^{(pre)}[t+1] &= dB_c^{(cur)}[t]
\end{aligned} \tag{58}$$

Step 45

The coefficients of the linear-phase FIR filter is
 5 found from the approximated amplitude characteristic (F
 105).

Namely, the coefficients of the linear-phase FIR
 filter is found from the amplitude characteristic
 obtained finally.

10 Fig.29 is a view illustrating frequency response
 characteristic of the low-pass filter obtained from the
 algorithms for finding "filter that satisfies the
 attenuation quantity of the stop band and that causes the
 signal to pass the frequency point of the transition
 15 band" on the basis of the algorithms for finding "filter
 having the minimum starting frequency of the stop band
 while taking the filter of the zero point for avoiding
 the chessboard distortion.

Fundamental algorithms, variables intended to find,
 20 and band of this case are as follows:

Fundamental algorithms

It is the Remez Exchange algorithms for finding the
 minimum starting frequency of the stop band that

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satisfies the attenuation quantity of the stop band.

- passing through (0.4π , 12 dB)
 - 24 taps
 - even symmetry
- 5 • $U = 3$ (filter coefficient is executed U times
such that DC gain becomes U)
- attenuation quantity of the stop band is not more
than - 40 dB

Variables intended to find

- 10 It is the end frequency ω_p of the pass band and the
starting frequency ω_s of the stop band.

[Table 6]

Band

15

band	Frequency region	gain	weight
Pass band	$0 \leq \omega \leq \omega_p$	1	1
Stop band	$\omega_s \leq \omega \leq \pi$	0	1

- 20 Further, in Fig.29, the solid line satisfies the
attenuation quantity of the stop band and indicates
frequency response of low-pass filter causing the
frequency point of the transition band to pass through.

- Furthermore, the black circle indicates the
25 designated frequency point. Also, dotted line indicates

frequency which becomes zero point for avoiding the chessboard distortion.

As known from Fig.29, the low-pass filter which is obtained from the algorithms for finding "filter that causes the signal to pass the frequency point of the transition band and that satisfies the attenuation quantity of the stop band" on the basis of "filter having the minimum starting frequency of the stop band" has good frequency response characteristic.

Subsequently, as for an algorithms on the basis of the algorithms for finding filter having the maximum end frequency of the pass band that satisfies the attenuation quantity of the stop band, explanation is made in relation to Fig.24, Fig.30 to Figs.33A and 33B.

The flowchart of this case is equivalent to Fig. 24 which is referred to in the algorithms for finding filter that causes the signal to pass the frequency point of the transition band and that satisfies the attenuation quantity of the stop band.

Namely, the present algorithms utilizes the algorithms for finding "filter having the maximum end frequency of the pass band that satisfies the attenuation quantity of the stop band".

The concrete course of the algorithms, as illustrated in Fig.30, ω_p is obtained with aforementioned algorithms

as inner loop, further loop for finding ω_s is put on outside thereof to determine parameter of the band.

Namely, the outside loop causes the starting frequency ω_s of the stop band to be fixed, while the
 5 inner loop causes the end frequency ω_p of the pass band to be found that satisfies the attenuation quantity dBs of the stop band.

When the amplitude characteristic thus found does not pass through the designated point (ω_c , dBc) of the
 10 transition band, ω_s is searched while using dichotomizing method like the case of searching "filter having the minimum starting frequency of the stop band that satisfies the attenuation quantity of the stop band".

Hereinafter, concrete algorithms is indicated,
 15 however, since the algorithms for finding "filter having the maximum end frequency of the pass band that satisfies the attenuation quantity of the stop band" to be the inner loop is the same as that described above, thus description thereof is omitted.

20 Also, the content of Fig.24 and each step processing F 102, F 103, F 104, and F 105 of the algorithms explained below, like the case of the first approach, is the same as the Remez Exchange algorithms taking into account the frequency response of the pre-filter
 25 explained in relation to Fig.6. Further, the content of

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each processing F 206, F 207, F 208, like the case of the second approach, is the same as processing explained in relation to Fig.11 namely the algorithms of "filter having the minimum starting frequency of the stop band
 5 that satisfies the attenuation quantity of the stop band". Accordingly, as for this processing, the same marks as Fig.6 and Fig.11 are used.

Step 50

As illustrated in Fig.24, firstly, initial setting is
 10 executed (F 301). In this initial setting, setting of the linear-phase FIR filter, setting of the band, setting of the coefficient of the pre-filter, setting of the initial extreme value point, designation of the attenuation quantity of the stop band, and setting of the initial
 15 frequency of dichotomizing method are executed.

Concrete items thus set are as follows:

- the number of tap
- linear-phase FIR filter with even symmetry or odd symmetry
- 20 • the number of the band is two
- the starting frequency of the pass band $\omega = 0$
- gain of the pass band
- the end frequency of the stop band $\omega = \pi$
- gain of the stop band
- 25 • weighting to the pass band and the stop band

- coefficient of the pre-filter
 - attenuation quantity dBs of the stop band (namely, pointing largeness δ_2 of ripple of the stop band)
 - frequency ω_c of the transition band and attenuation
- 5 quantity dBc thereof

• frequency $\omega^{(0)} = \omega_k^{(0)}$ ($k = 0, \dots, R$) that becomes the extreme value in the approximation band. Provided letter of right shoulder (i) expresses the number of repetition.

10 Also, Fig.31 is a view illustrating initial frequency of the dichotomizing method in the algorithms for finding filter that causes the signal to pass through the frequency point of the transition band, and that satisfies the attenuation quantity of the stop band.

15 As illustrated in Fig.31, in the present example, following values are given as the initial frequencies of the dichotomizing method.

$\omega_s^{(cur)}[0]$ = the vicinity of end frequency of the block

20 band (59)

The other side of $\omega_s^{(pre)}[0]$ is one which is found with the algorithms for searching "filter having the minimum starting frequency of the stop band that satisfies the

attenuation quantity of the stop band" as the value described later. Namely, ω_s which is found by the above algorithms is taken to be $\omega_s^{(pre)}[0]$.

$$\omega_p^{(pre)}[0] = \text{the vicinity of starting frequency of the pass band} \quad (60)$$

It should be noted that ω_p should be made to search as later described equation (61) essentially, however, ω_p that satisfies the attenuation quantity of the stop band can not be found. Accordingly, since the minimum value of the ω_p is degree of 0.01, the starting frequency ω_s of the stop band that satisfies the attenuation quantity of the stop band at this time is taken to be the initial frequency.

$$\omega_s^{(cur)}[0] = \text{the vicinity of } \omega_c \quad (61)$$

Portion of $[t]$ at the back of ω_s expresses the number of cycle.

Here, the Remez Exchange algorithms taking into account the frequency response of the pre-filter is executed to the frequency $\omega_s^{(pre)}[0]$, thus the maximum end frequency $\omega_p^{(pre)}[0]$ of the pass band that satisfies the

designated attenuation quantity dBs in the stop band is found, the gain $dB_c^{(cur)}[0]$ corresponding to ω_c at this time is found. The following steps are explained on the basis of this assumption.

5 Step 51

The algorithms for finding "filter having the maximum end frequency of the pass band that satisfies the attenuation quantity of the stop band" is executed (F 102, F 103, F 104, F206, F 207, F 208).

10 Concretely, in the processing F 102, interpolation polynomial expression is generated for interpolating an amplitude characteristic from the extreme value point at the time of $\omega_s^{(cur)}[t]$.

Subsequently, in the processing F 103, the new
15 extreme value point is determined from the amplitude characteristic obtained from the interpolation polynomial expression.

Then, in the processing F 104, repetition judgement of the Remez Exchange algorithms is executed.

20 Next, in the processing F 206, the minimum attenuation quantity is found in the stop band.

Next, in the processing F 207, end condition of the algorithms for finding filter having the minimum starting frequency ω_s of the stop band that satisfies the
25 attenuation quantity of the stop band is obtained.

[illegible][illegible][illegible][illegible][illegible][illegible][illegible]

[illegible]

(63)

Provided that ε_1 and ε_2 are extremely small values.

Step 44

5 Setting of the band is changed when result of the comparison does not satisfy equations (62) or (63), in the comparison between the frequency ωc of the transition band and the attenuation quantity dBc (F 311).

Concretely, the end frequency $\omega_s^{(cur)}[t+1]$ of new pass
10 band is made to set. Explanation is performed while
dividing into two cases of the first loop and the second
loop as the setting method.

First time:

In the case of the first time, there are three cases
15 illustrated in Figs.32A to 32C.

Namely, cases illustrated in Fig.32A, Fig.32B, and Fig.32C are considered to frequencies $\omega_s^{(pre)}[0] \omega_s^{(cur)}[0]$.

The case illustrated in Fig.32A is one in which the both satisfy the designated attenuation quantity dBc. In this case, the large frequency $\omega_s^{(cur)}[0]$ is taken to be solution, thus advancing toward the processing of Step 55.

The case illustrated in Fig.32B is one in which the both do not satisfy the designated attenuation quantity.

25 In this case, the present number of taps can not realize

the designated attenuation quantity. Accordingly, that effect is indicated to end.

The case illustrated in Fig.32C is one in which only one side satisfies the designated attenuation quantity. In this case, processing is moved to Step 51 in such a way as following equation (64).

Further, in the present method for giving initial frequency point, the case in which $\omega_s^{(cur)}[0]$ is satisfied and $\omega_s^{(pre)}[0]$ is not satisfied does not exist.

10

$$\begin{aligned}\omega_s^{(pre)}[1] &= \omega_s^{(cur)}[0] \\ \omega_s^{(cur)}[1] &= 0.5 \times (\omega_s^{(cur)}[0] + \omega_s^{(pre)}[0]) \\ dB_c^{(pre)}[1] &= dB_c^{(pre)}[0]\end{aligned}\tag{64}$$

Second time and later:

In the case of second time and later, two cases indicated in Figs.33A and 33B are considered. In the determining method of the new frequency $\omega_s^{(cur)}[t+1]$ in the second time and later, the frequency which satisfies the attenuation quantity dBc thus designated is preserved invariably within $\omega_s^{(pre)}[t+1]$. The case illustrated in Fig.33A, Fig.33B is considered to the frequencies

20

$$\omega_s^{(pre)}[t], \omega_s^{(cur)}[t].$$

The case illustrated in Fig.33A is one in which one side satisfies the designated attenuation quantity. In

this case, the processing is moved to next step 51 in such a way as the following equation (65).

Further, since the frequency that satisfies the designated attenuation quantity always conforms to
 5 $\omega_s^{(cur)}[t]$, the case that $\omega_s^{(pre)}[t]$ does not satisfy does not exist.

$$\begin{aligned}\omega_s^{(pre)}[t+1] &= \omega_s^{(pre)}[t] \\ \omega_s^{(cur)}[t+1] &= 0.5 \times (\omega_s^{(cur)}[t] + \omega_s^{(pre)}[t]) \\ dB_c^{(pre)}[t+1] &= dB_c^{(pre)}[t]\end{aligned}\quad (65)$$

10 The case illustrated in Fig.33B is a case that both satisfies designated attenuation quantity. In this case processing is moved to next step 51 in accordance with following equation (66).

$$\begin{aligned}\omega_s^{(pre)}[t+1] &= \omega_s^{(cur)}[t] \\ \omega_p^{(cur)}[t+1] &= \omega_s^{(cur)}[t] + 0.5 \times (\omega_s^{(cur)}[t] - \omega_s^{(pre)}[t]) \\ dB_c^{(pre)}[t+1] &= dB_c^{(cur)}[t]\end{aligned}\quad (66)$$

15

Step 55

The coefficients of the linear-phase FIR filter is found from the approximated amplitude characteristic (F 105).

20 Namely, the coefficients of the linear-phase FIR filter is found from the amplitude characteristic obtained finally.

Fig.34 is a diagram illustrating frequency response characteristic of the low-pass filter obtained from the algorithms for finding "filter that satisfies the attenuation quantity of the stop band and that enables the signal to be passed through the frequency point of the transition band" on the basis of the algorithms for finding "filter having the maximum end frequency of the pass band" with the filter of zero point for avoiding the chessboard distortion to be the pre-filter.

Fundamental algorithms, variables intended to find, and band of this case are as follows:

Fundamental algorithms

It is the Remez Exchange algorithms for finding the minimum starting frequency of the stop band that satisfies the attenuation quantity of the stop band.

- passing through (0.4 π , 12 dB)
- 24 taps
- even symmetry
- $U = 3$ (filter coefficient is executed U times such that DC gain becomes U)
- attenuation quantity of the stop band is not more than - 40 dB

Variables intended to find

It is the end frequency ω_p of the pass band and the

starting frequency ω_s of the stop band.

[Table 7]

Band

5

band	Frequency region	gain	weight
Pass band	$0 \leq \omega \leq \omega_p$	1	1
Stop band	$\omega_s \leq \omega \leq \pi$	0	1

10 Further, in Fig.34, the solid line satisfies the attenuation quantity of the stop band and indicates frequency response of low-pass filter causing the signal to be passed through the frequency point of the transition band.

15 Furthermore, the black circle indicates the designated frequency point. Also, dotted line indicates frequency which becomes zero point for avoiding the chessboard distortion.

As known from Fig.34, the low-pass filter which is
 20 obtained from the algorithms for finding "filter that causes the signal to be passed through the frequency point of the transition band and that satisfies the attenuation quantity of the stop band" on the basis of "filter having the minimum starting frequency of the stop
 25 band" has good frequency response characteristic.

Subsequently, the algorithms for designing of filter in order to find filter with the minimum number of tap that satisfies attenuation quantity of the stop band will be explained against the Remez Exchange algorithms with
 5 changeable band.

Here, the algorithms for obtaining filter having the minimum number of tap that satisfies attenuation quantity of the designated stop band will be explained against the algorithms for obtaining a filter that has the maximum
 10 end frequency ω_p of the pass band, which end frequency satisfies attenuation quantity of the stop band and against the algorithms for obtaining a filter having the minimum starting frequency ω_s of the stop band that satisfies attenuation quantity of the stop band.

15 Fig.35 is a view illustrating flowchart of the algorithms for finding filter with the minimum number of tap that realizes attenuation quantity of the stop band.

Here, free parameter of this algorithms, object, and principle of the algorithms thus enumerated are as
 20 follows:

* free parameter:

- it is the number of taps
- there exists two kinds of approaches.

Firstly, the end frequency ω_p of the pass band is made to be variable, and the starting frequency ω_s of the stop band is made to fix.

Secondly, the end frequency ω_p of the pass band
 5 is made to fix, and the starting frequency ω_s of the stop band is made to be variable.

* object: it is an object to obtain filter having the minimum number of tap that satisfies attenuation quantity dBs of the designated stop band to the algorithms in
 10 which one of the variables of the band is variable.

* principle: When being given no-solution in one time of loop, it is impossible to satisfy the attenuation quantity of the designated stop band because the number of tap is short, attempt is executed while increasing the
 15 number of tap by one.

Also, the content of Fig.35 and each step processing F 102, F 103, F 104, and F 105 of the algorithms explained below, like the case of the first approach, is the same as the Remez Exchange algorithms taking into
 20 account the frequency response of the pre-filter explained in relation to Fig.6. Further, the content of each processing F 201, F 206, F 207, F 208, like the case of the second approach, is the same as processing explained in relation to Fig.11 namely the algorithms of
 25 "filter having the maximum end frequency of the pass band

that satisfies the attenuation quantity of the stop band"
 and the algorithms of "filter having the minimum starting
 frequency of the stop band that satisfies the attenuation
 quantity of the stop band". Accordingly, as for this
 5 processing, the same marks as Fig.6 and Fig.11 are used.

Step 60

As illustrated in Fig.35, firstly, initial setting is
 executed (F 201). In this initial setting, setting of
 linear-phase FIR filter, setting of band, setting of
 10 coefficient of the pre-filter, setting of the initial
 extreme value point, designation of attenuation quantity
 of the stop band, and setting of initial frequency of
 dichotomizing method are executed.

Concrete items thus set are as follows:

- 15 • the number of tap
- linear-phase FIR filter with even symmetry or odd
 symmetry
- the number of the band is two
- the starting frequency of the pass band $\omega = 0$
- 20 • end frequency ω_p of the pass band in the case of
 the algorithms for finding "filter having the minimum
 starting frequency of the stop band that satisfies the
 attenuation quantity of the stop band.
- gain of the pass band
- 25 • the end frequency of the stop band $\omega = \pi$

• starting frequency ω_s of the stop band in the case of the algorithms for finding "filter having the maximum end frequency of the pass band that satisfies the attenuation quantity of the stop band.

- 5 • gain of the stop band
- weighting in connection with the pass band and the stop band

- coefficient of the pre-filter
- attenuation quantity dBs of the stop band (namely,
- 10 pointing largeness δ_2 of ripple of the stop band)

 • frequency $\omega^{(0)} = \omega_k^{(0)}$ ($k = 0, \dots, R$) that becomes the extreme value in the approximation band. Provided letter of right shoulder (i) expresses the number of repetition.

- 15 • input of initial frequency of dichotomizing method
- Step 61

The Remez Exchange algorithms taking into account the frequency response of the pre-filter is executed (F 102, F 103, F 104).

- 20 Concretely, in the processing F 102, the interpolation polynomial expression is generated for interpolating an amplitude characteristic from the extreme value point.

- Subsequently, in the processing F 103, the new
- 25 extreme value point is determined from the amplitude

characteristic obtained from the interpolation polynomial expression.

Then, in the processing F 104, repetition judgement of the Remez Exchange algorithms is executed.

5 Step 62

Next, the minimum attenuation quantity (the maximum weighted approximation error) of the stop band is obtained (F 206).

Step 63

10 Discrimination is executed whether or not the end
condition of the search of the frequency that satisfies
the attenuation quantity of the designated stop band
holds (F 207).

When the end condition holds, processing is moved to
15 Step 67 (F 105), while when the end condition does not
hold, processing is moved to Step 64 (F 208).

Step 64

When the end condition does not hold in connection with the search algorithms of the frequency that satisfies the attenuation quantity of the designated stop band, setting of the band is changed (F 208).

Step 65

Next, comparison to the attenuation quantity of the designated stop band is executed (F 414).

In the setting change of the band in the processing F
208, in the case of no solution at the one time loop
processing is moved to processing of Step 66 (F 414).
While with the exception of the aforementioned case,
5 processing is returned to processing of Step 61.

Step 66

One tap is increased (F 415).

One tap is increased in addition to the present
number of tap, thus processing is moved to initial
10 setting processing of Step 60 (F 201).

Step 67

The coefficients of the linear-phase FIR filter is
found from the approximated amplitude characteristic (F
105).

15 Fig.36 is a view illustrating frequency response
characteristic of the low-pass filter obtained from the
algorithms for finding "the minimum number of tap that
satisfies attenuation quantity of the stop band" while
taking the filter of the zero point for avoiding the
20 chessboard distortion.

Fundamental algorithms, variable intended to find,
and band of this case are as follows:

Fundamental algorithms

It is the Remez Exchange algorithms taking into
25 account frequency characteristic of the pre-filter for

finding the filter which has the minimum starting frequency of the stop band that satisfies the attenuation quantity of the stop band.

- even symmetry
- 5 • $U = 3$ (filter coefficient is executed U times such that DC gain becomes U)
- attenuation quantity of the stop band is not more than -60 dB

Variable intended to find

- 10 • it is the number N of tap.
- the starting frequency ω_s of the stop band.

[Table 8]

Band

15

band	Frequency region	gain	weight
Pass band	$0 \leq \omega \leq 0.3\pi$	1	1
Stop band	$\omega_s \leq \omega \leq \pi$	0	1

- 20 Further, in Fig.36, the solid line indicates frequency response of low-pass filter of the minimum number of tap (14 taps) in which the attenuation quantity of the stop band becomes not more than -60 dB.

- Furthermore, the dotted line indicated by ① indicates
 25 frequency which becomes zero point for avoiding the

chessboard distortion, and the dotted line indicated by
 ② indicates period of the band given beforehand.

As seen from Fig.36, the low-pass filter which is
 obtained from the algorithms for finding "the minimum
 5 number of tap which realizes attenuation quantity of the
 stop band" has good frequency response characteristic.

Furthermore, Fig.37 is a view illustrating frequency
 response characteristic of the low-pass filter obtained
 from the algorithms for finding "the minimum number of
 10 tap that satisfies attenuation quantity of the designated
 stop band" while taking the filter of the zero point for
 avoiding the chessboard distortion.

Fundamental algorithms, variable intended to find,
 and band of this case are as follows:

15 Fundamental algorithms

It is the Remez Exchange algorithms taking into
 account frequency characteristic of the pre-filter for
 finding the filter which has the maximum end frequency of
 the pass band that satisfies the attenuation quantity of
 20 the stop band.

- even symmetry
- $U = 3$ (filter coefficient is executed U times
 such that DC gain becomes U)
- attenuation quantity of the stop band is not more

25 than - 60 dB

Variable intended to find

- it is the number N of tap.
- the starting frequency ω_s of the stop band.

5

[Table 9]

band	Frequency region	gain	weight
Pass band	$0 \leq \omega \leq \omega_p$	1	1
Stop band	$0.5\pi \leq \omega \leq \pi$	0	1

10

Further, in Fig.37, the solid line indicates frequency response of low-pass filter of the minimum number of tap (15 taps) in which the attenuation quantity of the stop band becomes not more than -60 dB.

- 15 Furthermore, the dotted line indicated by ① indicates frequency which becomes zero point for avoiding the chessboard distortion, and the dotted line indicated by ② indicates period of the band given beforehand.

As known from Fig.37, the low-pass filter which is
 20 obtained from the algorithms for finding "the minimum number of tap which realizes attenuation quantity of the designated stop band" has good frequency response characteristic.

Subsequently, as the second modified example,
 25 explanation is performed about algorithms for finding

filter with the minimum numbers of tap that enables the signal to be pass through frequency point of transition band that satisfies attenuation quantity of the stop band.

5 Here, algorithms for finding filter with the minimum number of tap that satisfies the attenuation quantity of the block band and and that enables the signal to be passed through frequency point of transition band and to the algorithms for finding "filter that satisfies the
10 attenuation quantity of the block band and and that enables the signal to be passed through the frequency point of the transition band".

Fig.38 is a view illustrating flowchart of the algorithms for finding filter with the minimum number of
15 tap that satisfies the attenuation quantity of the stop band and that enables the signal to be passed through the frequency band of the transition band.

Here, free parameter of this algorithms, object, and principle of the algorithms thus enumerated are as
20 follows:

* free parameter:

- it is the number of taps
- the end frequency ω_p of the pass band.
- the starting frequency ω_s of the stop band

* object: it is an object to obtain filter having the minimum number of tap that satisfies attenuation quantity dBs of the designated stop band and that the attenuation quantity dBc is passed at the frequency ω_c of the transition band. Namely, the maximum end frequency ω_p of the pass band so as to become the attenuation quantity dBc at the designated frequency ω_c of the transition band and the minimum starting frequency ω_s of the stop band are determined to obtain the filter with the minimum number of tap..

* principle: When being given no-solution in one time of loop, it is impossible to satisfy the attenuation quantity because the number of tap is short, attempt is executed while increasing the number of tap by one. Further, in cases where it is impossible to realize the frequency point of the transition band, attempt is executed while increasing the number of tap by one.

Also, the content of Fig.38 and each step processing F 103, F 104, and F 105 of the algorithms explained below, like the case of the first approach, is the same as the Remez Exchange algorithms taking into account the frequency response of the pre-filter explained in relation to Fig.6. Further, the content of each processing F 201, F 206, F 207, F 208, like the case of the second approach, is the same as processing explained

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in relation to Fig.11 namely the algorithms of "filter having the maximum end frequency of the pass band that satisfies the attenuation quantity of the stop band" or the algorithms of "filter having the minimum starting frequency of the stop band that satisfies the attenuation quantity of the stop band". Further, the contents of the processing F 301, F 309, F 310, and F 311 are the same as the processing explained in relation to Fig.24, namely, the same as the algorithms for finding the filter that satisfies the attenuation quantity, and, in which designated attenuation quantity is passed through at the designated frequency of the transition band. Accordingly, as for this processing, the same marks as Fig.6 Fig.11 and Fig.24 are used.

15 Step 70

As illustrated in Fig.38, firstly, initial setting is executed (F 301). Concretely, initial setting of the algorithms is executed for finding the filter that satisfies the attenuation quantity of the stop band, and in which designated attenuation quantity is passed through of the transition band.

Concrete items thus set are as follows:

- the number of tap
- linear-phase FIR filter with even symmetry or odd symmetry

- the number of the band is two
- the starting frequency of the pass band $\omega = 0$
- gain of the pass band
- the end frequency of the stop band $\omega = \pi$
- 5 • gain of the stop band
- weighting to the pass band and the stop band
- coefficient of the pre-filter
- attenuation quantity dBs of the stop band (namely, pointing largeness δ_2 of ripple of the stop band)
- 10 • frequency ω_c of the transition band and attenuation quantity dBc thereof
- frequency $\omega^{(0)} = \omega_k^{(0)}$ ($k = 0, \dots, R$) that becomes the extreme value in the approximation band. Provided letter of right shoulder (i) expresses the number of
- 15 repetition.
- input of initial frequency of dichotomizing method.

Step 71

The Remez Exchange algorithms taking into account the frequency response of the pre-filter is executed (F 102, 20 F 103, F 104).

Concretely, in the processing F 102, interpolation polynomial expression is generated for interpolating an amplitude characteristic from the extreme value point.

Subsequently, in the processing F 103, the new 25 extreme value point is determined from the amplitude

[illegible][illegible][illegible][illegible][illegible][illegible][illegible][illegible][illegible][illegible][illegible]

In change of the setting of the band in the processing F 208, in the case of no solution at the one time of the loop, processing is moved to processing of Step 76 (F 415). In the cases with the exception of the
 5 aforementioned case, processing is returned to processing of Step 71.

Step 76

One tap is increased (F 415).

One tap is increased in addition to the present
 10 number of tap, thus processing is moved to initial setting processing of Step 70 (F 301).

Step 77

When the end condition of the search algorithms of the frequency that satisfies designated attenuation
 15 quantity of the stop band holds, attenuation quantity of the frequency which is designated to the transition band is examined (F 309).

Comparison between the attenuation quantity of the designated stop band and obtained attenuation quantity is
 20 performed (F 414).

When the end condition holds, processing is moved to Step 82 (F 105), while when the end condition does not hold, processing is moved to Step 79 (F 311).

Step 79

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When the end condition does not hold, setting of the band is changed (F 311).

Step 80

Next, comparison between the attenuation quantity of
5 the designated stop band and obtained attenuation
quantity is executed (F 416).

In change of the setting of the band in the
processing F 311, in the case of no solution at the one
time of the loop, processing is moved to processing of
10 Step 81 (F 417). In the cases with the exception of the
aforementioned case, processing is returned to processing
of Step 71.

Step 81

One tap is increased (F 417).

15 One tap is increased in addition to the present
number of tap, thus processing is moved to initial
setting processing of Step 70 (F 301).

Step 83

The coefficients of the linear-phase FIR filter is
20 found from the approximated amplitude characteristic (F
105).

Fig.39 is a diagram illustrating frequency response
characteristic of the low-pass filter obtained from the
algorithms for finding "filter with the minimum number of
25 taps which filter satisfies the attenuation quantity of

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the stop band, and which filter enables the signal to be passed through the frequency point of the transition band" with the filter of zero point for avoiding the chessboard distortion to be the pre-filter.

- 5 Fundamental algorithms, variable intended to find, and band of this case are as follows:

Fundamental algorithms

10 It is the Remez Exchange algorithms for obtaining a filter that enables the signal to be passed through the frequency point of the transition band on the basis of the algorithms for obtaining the filter that satisfies the attenuation quantity of the stop band that has the maximum end frequency of the pass band.

- passing through (0.4π , 12 dB)
- 15 • even symmetry
- $U = 3$ (filter coefficient is executed U times such that DC gain becomes U)
- attenuation quantity of the stop band is not more than - 60 dB

20 Variable intended to find

- it is the number of taps N .
- the end frequency ω_p of the pass band.
- the starting frequency ω_s of the stop band.

[Table 10]

band	Frequency region	gain	weight
Pass band	$0 \leq \omega \leq \omega_p$	1	1
Stop band	$\omega_s \leq \omega \leq \pi$	0	1

Further, in Fig.39, the solid line indicates frequency response of low-pass filter of the minimum number of tap (17 taps) in which the attenuation quantity of the stop band becomes not more than -60dB, and the attenuation quantity becomes not more than -12dB on the frequency 0.4π of the transition band. Further, dotted line indicates the frequency that becomes zero point in order to avoid the chessboard distortion, the black circle indicates the designated frequency point of the transition band.

As seen from Fig.39, the low-pass filter which is obtained from the algorithms for finding "filter with the minimum number of taps which filter satisfies attenuation quantity of the stop band, and which filter enables the signal to be passed through the frequency point of the transition band" has good frequency response characteristic.

As described-above, according to the present invention, there is an advantage that is possible to

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